

DERIVATION OF MATERIAL BALANCE EQUATION
(above the bubble point - no water influx)

Original oil vol. = current oil vol. + formation compression & water expansion

$$N B_{oi} = (N - N_p) B_o + \frac{N B_{oi}}{(1 - S_w)} (C_f + S_w C_w)(p_i - p)$$

$$\text{let } \bar{c} = \frac{C_f + C_w S_w}{(1 - S_w)}, \text{ then}$$

$$N B_{oi} = N B_o - N_p B_o + N B_{oi} \bar{c} (p_i - p)$$

$$N = \frac{N_p B_o}{(B_o - B_{oi} (1 - \bar{c}) (p_i - p))}$$

N_p - cumulative oil production (stock tank barrels)

N - original oil in place (stock tank barrels)

B_o - oil formation volume factor (reservoir bbls./stock tank bbls.)

B_{oi} - initial formation volume factor (reservoir bbls./stock tank bbls.)

p - reservoir pressure (psia)

p_i - initial reservoir pressure (psia)

C_f - formation compressibility (psi^{-1})

C_w - water compressibility (psi^{-1})

S_w - water saturation (fraction)

SRC

11

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