BENSON-MONTIN-GREER DRILLING CORP. EXHIBITS IN CASE NOS. 7980, 8946, 8950 AND 9111 BEFORE THE OIL CONSERVATION COMMISSION OF THE NEW MEXICO DEPARTMENT OF ENERGY AND MINERALS

JUNE 13, 1988

ESPORE THE OIL CONSERVATION COMMISSION NE CONSERVATION COMMISSION Senta Fe, New Mexico Case No.9111, 9412 Exhibit No. 2 . ub Litted by BMG rearing Date JUNE 13, 1988

NIOBRARA MEMBER OF THE MANCOS FORMATION WEST PUERTO CHIQUITO AND BOULDER POOLS

Gravity drainage is succinctly summarized by Frick (Reference 1) in two paragraphs as icuitons: "Gravity drainage is the self-propulsion of oil downward in the reservoir rock. Under favorable conditions it has been found to effect recoveries of 60 per cent of the oil in place, which is comparable with or exceeding the recoveries normally obtained by water drive. Gravity is an ever-present force in oil fields that will drain oil from reservoir rock from higher to lower levels wherever it is not overcome by encroaching edge water or expanding gas.

Gravity drainage will be most effective if a reservoir is produced under conditions which allow flow of oil only or counterflow of oil and gas.

- This may be attained under pressure maintenance by crestal-gas injection, which keeps the gas in solution, or ..**.**i
- It may be attained by a gradual reduction in pressure, so that the oil and gas can segregate continuously by counterflow. 3
- It may also be obtained by first producing the reservoir under a depletion-type mechanism until the gas has been practically exhausted, then by gravity drainage. ÷

gravity drainage will be found in the discussion of the many aspects of gravi (Method numbers and emphasis supplied.) classic paper by Lewis." thorough 4

In the fractured Niobrara, because of its unfavorable Kg/Ko relation and the exceptionally high rate of decline of oil productivity with declining pressures and increasing GOR's the third method of obtaining gravity drainage described by Frick (first depleting the reservoir by solution gas drive and then attempting gravity drainage) is not economically available since the at oil production in this formation, following depletion by solution gas drive, is economically unattractive rates, if not below the economic limit. rate of

When we examine the fundamental flow relations along with the cost of gas crestal gas injection, or low production rates. When we examine the fundamental flow relations along with the con-injection, it becomes immediately apparent that crestal gas injection is the better method. This leaves for the Niobrara, then, the other two methods:

DETAILS OF ANALYSIS

The relation of the flowing fluids with, and without, gravity drainage is given by the Buckley-Leverett fractional flow equation (Reference 2).

where d= (b-2) Z KAQ . 488 Iŧ

When fg is zero, maximum gravity drainage occurs (Reference 2). Under this condition the value of the denominator then becomes insignificant. By dropping the denominator, substituting hw for A, Koh for K(Kro) and (qp) (Bt) for qt (then W becomes the width along the strike) and solving for qt when fg = 0, the equation becomes:

$$q_0 = \frac{.488 \text{ Koh d sin}}{.000 \text{ M}}$$

We then recognize that this is the Conservation Commission in Case 3455, B-M-G Exhibit 2, Appendix II, Part B, December 1969, which When there is no free gas B_t = B = FVF for oil. We then recognize that this is the same formula, derived directly from Muskat's (Reference 3) basic analyses, and provided the Oil 15:

$$q_0 = \frac{2580 \text{ Koh d since}}{u_0 B_t}$$
 Where $q_0 = BOPD$ per linear mile along the strike Koh = darcy feet darcy feet

(where W = 5280, distance along strike)

11

J

On the following pages, the Boulder Pool production is compared with its gravity drainage potential as determined by the above formula. The formation dip in Boulder varies from 1000'/mile to 1500'/mile. (See plat following and Appendix III).







• .

The Boulder Pool was well positioned to obtain gravity drainage recoveries: steep dip, short distance downdip, high transmissibility and crestal gas cap. (Reference Appendix - Part III).

BOULDER MANOS POOL COMPARISON OF OIL PRODUCTION RATES GRAVITY DRAINAGE POTENTIAL HI.IM

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Gravity Drainage Rate for Koh: 10 20 30 d-ft d-ft d-(13) (14) (1 2000 1000 1000 500 Rocentrir Temperature 140⁰ ק Dip 1250'/Mile Field Oil Prod. Bbls/Mo. Rate** (11) (12) 108 300 13,000 36,000 Total Res. Bbl. Per Stock Tank Bbl (10) 1.54 2.95 650 8) 6 300 2580 Krh d sin A U Bt Res. Bbls. Per MCF (8) 2.91 3.70 $\frac{\text{Vis}}{(7)}$ (travity drainage motential = WDU/linear mile along strike = 3.1 3.1 d = S.G. Oil Minus <u>S.G. Gas</u> (6) .77 .78 S.G.* Gas (5) .05 .04 S.G.* 0i1 (4) .82 .82 .88 .90 ∾I? Press. (Psia) (2) 930 750 5-01-63 3-01-62 Uate (1)

* Specific gravity (water = 1.0)

** BOPD per linear mile along strike

*** Peak (JOR

Reservoir fluid properties from bottom hole sample analysis (Appendix Part I).

***09

300

200

1500 600

> 400 40

200 20 100

300 108 45

36,000 13,000 5,400

7.33

1400 4000

4.81 14.9 30

3.3 4.2 4.5

.79

.03 .01 ł

.82 .82

.92 . 97

590 200

2-01-64 6-13-65

10 8

300

.82 .81

.82

.98

est 100

1970

3000

30 d-ft (15)

CANADA OUITOS UNIT

Boulder oil recoveries were substantially through gravity drainage; and investigation was made to It was recognized that determine if Canada Ojitos Unit production might also receive this high gravity drainage recovery Initial development in Canada Ojitos Unit was concurrent with Boulder.

For the Canada Ojitos Unit oil characteristics, dip of 200° to 400° per mile and measured transmissibility (Koh) of 5 to 10 darcy feet (by interference tests) it was determined that the gravity drainage potential was in the range of 400 to 800 BOPD per linear mile along the strike.

contact, meaning that the 400 to 800 BOPD must be shared by wells in a 5 or 6 square mile section of Also unless pressure was maintained, the gravity drainage rate would decrease as This was not as high as Boulder but high enough for commercial operation of the reservoir providing it was not overdriiled. One of the problems was the 5 to 6 mile downdip section below the gas-oil pressure declined and free gas developed. the reservoir.

low recovery; and the depletion mechanism would deteriorate to solution gas drive If produced by solution gas drive the poor relative permeability characteristics would mean an unless the withdrawal rates were kept low and pressure maintained. exceptionally

mechanism is primarily solution gas drive and the pressures and GOR's are typical for fractured formations. Note that the potential commences at about 800 barrels per day per linear mile along the strike but drops rapidly to less than 200 and is negligible when the GOR reaches 8,000 to 10,000. Accordingly it is clear that if the producing mechanism be allowed to deteriorate to that of On the next two pages are schedule and graph showing gravity drainage potential if the producing solution gas drive that the gravity drainage share will be rather small. POTENTIAL GRAVITY DRAINAGE RATES CANADA OJITOS UNIT

Gravity drainage potential = BOPD/linear mile along strike = 2580 Koh d sin o U Bt

Dìp 200'/Mile

TABLE A - FOR 'TYPICAL PRESSURE AND GAS-OIL RATIOS UNDER SOLUTION GAS DRIVE

Gravity Drainage Rate *** for Koh = 10 darcy feet (11)	1000	700	240	190	110	38	13	1 1 1 1 1 8 8 1 1		675	540	440	340	
Total Reservoir Bbls per Stock Tank Bbl (BT) (10)	1.54	1.30	4.13	5.26	8.78	23	58	, , , , , , , , , , , , , , , , , , ,		1.48	1.85	1.97	2.55	
<u>86</u>	300	500	1500	2500	4000	8000	14000	1 1 1	SNDITIONS	600	800	600	800	
Res. Bbls. Per MCF (8)	2.91	1.83	1.90	1.98	2.14	2.88	4.14	1 1 1	- FOR OTHER O	1.83	1.83	2.88	2.88	
vis (7)	3.1	.62	.63	.64	.67	.76	.88	1 1 1	TABLE B	.62	.62	.76	.76	
u - S.G. Oil Minus S.G. Gas (6)	.77	.635	. 638	.641	.647	.676	.695	1 9 1 9		. 635	. 635	.76	.76	
S.G.* Gas (5)	.05	.085	.082	670.	019	.054	.045	1		.085	.085	.054	.054	
S.G.* 0i1 (4)	.82	.72	.72	.72	.72	.73	.74	1 1 1		.72	.72	.73	.73	
2 <u>(</u>	.88	.85	.85	.855	.860	.890	.895	1 1 1		.85	.85	.89	.89	
Press. (<i>P</i> sia) (2)	930	1500	1450	1400	1300	1000	700	1 1 1		1500	1500	1000	1000	

ł

* Specific gravity (water = 1.0)

** BOPD per linear mile along strike

Reservoir fluid properties from bottom hole sample analysis (Appendix Part II).



THERE IS ONLY ONE GRAVITY DRAINAGE RATE AVAILABLE FOR A TYPICAL SECTION OF THE RESERVOIR

The sketch on the facing page illustrates this fact of gravity drainage.

Note that if a well has the ability to produce the gravity drainage potential of a one mile wide section of the reservoir, that the drilling of additional wells will not increase the reservoir gravity drainage ability; but in fact if they are produced in addition to the initial well they will serve to reduce the ultimate recovery by causing the producing mechanism to deteriorate to that of solution gas drive. SCHEMATIC GRAVITY DRAINAGE SYSTEM (Fracture Blocks Omitted)



HISTORY OF GRAVITY DRAINAGE CANADA OJITOS UNIT

barrels of oil. That this is a fact is attested to by the low GOR's of the recovery wells while the reservoir has been operated under pressure maintenance by gas injection. The Canada Ojitos Unit has produced efficiently under the gravity drainage mechanism several million

If gravity drainage were not operative, then the producing mechanism under gas injection would be simply that of "gas drive"; and under gas drive without gravity segregation, the low viscosity of the gas would cause it to permeate the reservoir, in accordance with the fractional flow relations, with early high GOR's (Reference 4, and others).

Any oil "bypassed" during the first gravity drainage phase of high pressure gravity drainage depletion will be recovered later during low pressures (Reference 4).

When the above facts are recognized, two important characteristics of this reservoir are evident:

- A large proportion of the reservoir volume is in high capacity fractures (otherwise the injected gas would have displaced the small fracture volume early in the producing life). ŗ.
- Gravity segregation has been significant (even with the large volume in the fracture system, injected gas, if operating only under "gas drive" would have caused early high GUR's). 2

APPENDIX

- Part I: Reservoir Fluid Analysis Boulder Pool (pink).
- Part II: Reservoir Fluid Analysis Canada Ojitos Unit (green).
- Part III: Oil and Gas Fields of the Four Corners Area, Four Corners Geological Society, Volume I, Pages 248-250, 1978 (blue).

October 23, 1962

RESERVOIR FLUID DIVISION

Standard Oil Company of Texas Drawer S Monahans, Texas

> Subject: Reservoir Fluid Study Jicarilla 4-26 No. 3 Well Boulder Mancos Field Rio Arriba County, New Mexico Our File Number: RFL 2301

Gentlemen:

Subsurface fluid samples were collected from the subject well by a representative of Core Laboratories, Inc. and submitted to our Dallas laboratory for use in a reservoir fluid study. The results of this study are presented on the following pages.

The saturation pressure of the fluid was measured to be 802 psig at the reservoir temperature of 141° F. The reservoir pressure at the sampling depth is 856 psig.

During differential pressure depletion the fluid evolved 147 standard cubic feet of gas per barrel of residual oil. The associated formation volume factor was measured to be 1.098 barrels of saturated fluid per barrel of residual oil. The viscosity of the fluid was measured under similar depletion conditions. It varied from a minimum of 3.03 centipoises at the saturation pressure to a maximum of 5.44 centipoises at atmospheric pressure.

It was a pleasure to perform this study for you. If you have any questions or if we may assist you further, please do not hesitate to contact us.

Very truly yours,

Core Laboratories, Inc. Reservoir Fluid Division P. L. Moses

a. C. Carnes, J.

			Page_	10	f <u> 11 </u>
			File	RFL	2301
Commany	Standard Oil Company of Texas	Date Sampler	d October	4, 196	2
Well	Jica: illa 4-26 No. 3	County	Rio Arr	iba	•
Tiald	Boulder Mancos		New Me	xico	
Formation	FORMATION CAR	RACTERISTI	CS Gallup		
Date First	Well Completed	-	August		19 60
Original R	leservoir Pressure	-	867	PSIG @	3880 Ft
Original P	roduced Gas-Oil Ratio	-	167		SCF/Bb
Pro	duction Late	-	175		Bbl/Day
Sen	arator Pressure and Temperature			PSIG.	°F
Oil	Gravity-at 60° F.	-	32.5		°API
Datum		_			Ft. Subsea
Original G	as Cap	-			
	WELL CHARA	CTERISTICS			
Elevation		-	7240 GL		Ft.
Total Dep	th	-	4120		Ft.
Producing	Interval	-	3820-4120		Ft.
Tubing Siz	ze and Depth	•		In. to	Ft.
Productivi	ty Index	-	Bbl/I	D/PSI @	Bbl/Day
Last Rese	rvoir Pressure		867	PSIG @ .	<u>3880</u> Ft.
Dat	ie	-	October 4		<u> </u>
Res	servoir Temperature	-	<u>139*</u> ºI	F. @	<u>3880</u> Ft.
Sta	tus of Well	-	Shut in 65 h	<u>iours</u>	
Pre	ssure Gauge	-	Amerada ()	00)	
Normal Pr	roduction Rate	-	1/5		Bbl/Day
Gas	s-Oil Ratio	-	200		SCF/Bbl
Sep	arator Pressure and Temperature	-	F	PSIG,	°F.
Bas	se Pressure	-	<u>15.025</u>	····	PSIA
Well Maki	ng Water	-	None		% Cut
	SAMPLING C	ONDITIONS	•		
Sampled a	t	_	3850		Ft.
Status of V	Well	-	Shut in 65 l	nours	
Gas	s-Cil Ratic				SCF/Bbl
Sep	parator Pressure and Temperature	-	F	PSIG,	°F
Tui	bing Pressure		4		PSIG
Cas	ing Pressure	-			PSIG
Core Labo	ratories Engineer	-	NT		
Type Sam	pler	-	Perco		
	,				

REMARKS:

* Temperasure extrapolated to mid-point of producing interval = 141° F.

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Page_	2	of	11		
File	RF	L 23	01		
Well	Jic	arilla	4-26	No.	3
W CII				/ 7	
	574,	YCAA	2 <i>0 –</i>	4 7.	C KA-
1	9au	LDER	e A		~

<u>0.01959 @ 141 °F.</u>

VOLUMETRIC DATA OF Reservoir Fluid SAMPLE

1. Saturation pressure (bubble-point pressure)802 PSIG @ 141 °F.2. Thermal expansion of saturated oil @ 5000 PSI = $\frac{V @ 141 °F}{V @ 76 °F} = 1.02778$ 3. Compressibility of saturated oil @ reservoir temperature: Vol/Vol/PSI:From 5000 PSI to 3500 PSI = 5.27×10^{-6} From 3500 PSI to 2000 PSI = 5.92×10^{-6}

These analyses, opinions or interpretations are based on observations and material supplied by the client to whom, and for whose exclusive and confidential use, his report is made. The interpretations or opinions expressed represent the best judgment of fore Laboratories The fall errors and emissions expressed is but

From <u>2000</u> PSI to <u>802</u> PSI = 6.63×10^{-6}

4. Specific volume at saturation pressure: ft ³/lb

- 01959 = 51.05 #/4+3 ->,3545 #/in=/4+

CORE LABORATORIES, INC.

Petroleum Reservoir Engineering

DALLAS, TEXAS

Page_	_3	of	11		_
File	<u>RFL</u>	2301			
Well	Jica	rilla 4-	26 No.	3	

Reservoir Fluid SAMPLE TABULAR DATA

	PRESIURE-VOLUME	VISCOSITY	DIFFERENT	IAL LIBERATION @	141 °F.
PRESSURE PSI GAUGE	@ 141 °F., RELATIVE VOLUME OF OIL AND GAG. V/VEAT.	OF OIL @ 141°F., CENTIPOISES	GAS/OIL RATIO LIBERATED PER BARREL OF RESIDUAL OIL	GAS/OIL RATIO IN SOLUTION PER BARREL OF RESIDUAL OIL	RELATIVE OIL VOLUME, V/VR
5010		4 52			
5000	0.9755	1, 54			1 071
4505	•	. 4. 33			1.011
4500	0,9780				1.074
4000	0,9806	4,15			1.077
3500	0, 9833	3.96			1 080
3010		3, 75			1.000
3000	0.9861				1.083
2510	,	3, 60			1,005
2500	0, 9890	51.00			1 086
2005		3, 42	•		
2000	- 0.9921	•• - -	1		1.089
1505		3.26			21.007
1500	0.9953	•••=•			1,093
1400	0.9960				1.094
1300	0.9967				1.094
1200	0.9973				1.095
1100	0.9980				1,096
1015		3.10			
1000	0.9987				1.097
900	0.9994				1.097
802	1.0000	3.03	0	147	1.098
798	1.0016		-		,.
794	1.0032			•	
790	1.0062				
777	1.0139				
755		3.09			
751	1.0293				•
712	1.0477				
698			19	128	1.092
663	1.0795		·		
655		3.20			
603	1.1268			. •	

v = Volume at given pressure

/sat. = Volume at saturation pressure and the specified temperature.

/a = Residual oil white me at 14.7 PSI absolute and 60° F.

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File	RFL 2301	
Well	Jicarilla 4-26 No. 3	

Reservoir Fluid SAMPLE TABULAR DATA

	PRESIURE.VOLUME	VISCOSITY	DIFFERENT	IAL LIBERATION @	141 °F.
PRESSURE PSI GAUGE	© 141 °F., RELATIVE VOLUME OF OIL AND GAS, V/VEAT.	OF OIL Ultited Iters CENTIPOISES	GAS/OIL RATIO LIGERATED PER BARREL OF RESIDUAL OIL	GAS/OIL RATIO IN SOLUTION PER BARREL OF RESIDUAL OIL	RELATIVE OIL VOLUME, V/VR
 ć01			34	113	1.087
550		3.37			
538	1. 1915				
499			50	97	1.081
473	1.2765				
455		3.52			
404	1.3966				
398			67	80	1.075
350		3.78			
342	1.5473			•	
300			83	64	1.069
276	- 1.7859				
250		4.06			
200	2.2504				
199			100	47	1.062
150		4.38			
138	3.0146				
98			119	28	1.055
50		4.82			
0	•	5.44	147	0 @60°F	1.036 . = 1.000

Gravity of residual oil = 30.5° API @ 60° F.

v = Volume at given pressure

/sar. = Volume at saturation pressure and the specified temperature.

/* = Residual oil volurne at 14.7 PSI absolute and 60° F.

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Well	Jicarilla 4-26 No. 3

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Differential Pressure Depletion at 141° F.

Pressure PSIG	Oil Density Gms/Cc	Gas Gravity	Deviation Factor
802	0.8176		
698	0.8199	0.686	0.934
601	0,8218	0.687	0.940
499	. 0,8242	0.689	0,950
398	0.8265	0.699	0,958
300	0.8287	0.714	0.968
199	0.8314	0.743	0.979
98	0.8340	0.806	
0.	0.8428	1.093	

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File	RFL	2301		

Well Jicarilla 4-26 No. 3

SEPARATOR TESTS OF Reservoir Fluid SAMPLE

SEPARATOR PRISSURE. PSI GAUGE	SEPAR; TOR TEMPERATURE, • F	SEPARATOR GAS/OIL RATIO See Foot Note (1)	STOCK TANK GAS/OIL RATIO See Foot Note (1)	STOCK TANK Gravity, • Api @ 60• F.	SHRINKAGE FACTOR, Vr/V5AT. See Foot Note (2)	FORMATION VOLUME FACTOR, VSAT./VR See Foot Note (3)	SPECIFIC GRAVITY OF FLAGHED GAS
0	74	155		30.5	0.9033	1.107	0.885
30	74	138	10	30.7	0.9102	1.099	
60	74	127	20	30.7	0.9099	1.099	
120	74	111	40	30.7	0.9074	1.102	

- (1) Separator and Stock Tank Gas/Oil Ratio in cubic feet of gas @ 60° F. and 14.7 PSI absolute per barrel of stock tank oil @ 60° F.
- (2) Shrinkage Factor: VR/VEAT. is barrels of stock tank oil @ 60° F. per barrel of saturated oil @ 802 PSI gauge and 141 ° F.
- (3) Formation Volume Factor: Vany./Va is barrels of saturated oil @ 802 PSI gauge and 141 ° F. per barrel of stock ank oil @ 60° F.

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		File RFL 2301
Staniard Oil Company of Texas	_ Formation_	Gallup
Jicarilla 4-26 No. 3	_ County	Rio Arriba
Boulder Mancos	State	New Mexico

State_

HYDROCAREON ANALYSIS OF Reservoir Fluid SAMPLE

Company_

Well

Field

COMPONENT	WEIGHT PER CENT	MOL PER CENT	DENSITY @ 60° F. Grams Per Cubic Centimeter	• API @ 60• F.	MOLECULAR WEIGHT
Hydrogen Sulfide					
Carbon Dioxide	0.33	1.50			
Nitrogen	0.04	0.26			
Liethane	1.38	17.21			
Ethane	0.63	4.17			
Propane	0.22	0.97			
iso-Butane	0.10	0.35			
n-Butane	0.11	0.37			
iso-Pentane	0.31	0.86			
n-Pentane	0.45	1.25			
Hexanes	0.97	2.25			
Heptanes plus	95.46	70.81	0.8771	29.7	269
	. 100.00	100.00			

hese analyses, opinions or interpretations are based on observations and material supplied by the client to whom, and for whose exclusive and confidential use, is report is made. The interpretations or opinions expressed represent the cest judgment of Core Laboratories, Inc. (all errors and omissions excepted); but

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Core Laboratories, Inc. Reservoir Fluid Division -

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a. C. Carnes, Sp.

A. C. Carnes, Jr. Senior Engineer

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File	RFL	23	01

PRESSURE-VOLUME RELATIONS OF RESERVOIR FLUID

Com	my Standard	i Gil Co. of T	exas	Formation _	Gallup	
Well	Jicarilla	a 4-26 No. 3		_County	<u>Rio Arriba</u>	
Field	Boulder	Mancos		State	New Mexico	
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	500	1000	1500	2000	2500	3000
v						-

PRESSURE: POUNDS PER SQUARE INCH GAUGE

·**L**



160

140

120

100

80

60

40

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PRESSURE. POUNDS PER SQUARE INCH GAUGE

2000

2500

÷.,

1 ÷

1500

1000

1.16

1.14

1.12

1.10

1.08

1.06

1.04

1.02

1.00

. .

3000

CORE LABORATORIES, INC. Petroleum Reservoir Engineering DALLAS, TEXAS Viscosity of Reservoir Fluid

Company Standard Oil Co. of Texas Formation

Jicarilla 4-26 No. 3_____County_

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0.0

0

Well____

Page _	10	of <u>11</u>
File	RFL	2301

	Field	Boulder	Mancos	Sta	:te <u>N</u>	<u>ew Mexico</u>	
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Gallup Rio Arriba

Pressure: PSIG

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1000

500

2000

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July 27, 1965

RESERVOIR FLUID DIVISION

.....

Benson-Montin-Greer Drilling Corporation 158 Petrcleum Center Building Farmington, New Mexico

Attention: Mr. Albert R. Greer

Subject: Reservoir Fluid Study Bolack-Greer Inc. ב-11 בשנה Canada Ojitos Unit No. 12-11 Well Puerto Chiquito Field Rio Arriba County, New Mexico Our File Number: RFL 3366

Gentlemen:

Subsurface fluid samples were collected from the subject well by a representative of Core Laboratories, Inc. and were delivered to our laboratory in Dallas for use in a reservoir fluid study. The results of this study are presented on the following pages.

The saturation pressure of the fluid was found to be 1519 psig at the reservoir temperature of 162° F. The associated formation volume factor was found to be 1.297 barrels of saturated fluid per barrel of residual bil. By differential pressure depletion the fluid evolved 478 standard cubic feet of gas per barrel of residual oil. Under similar depletion conditions the viscosity increased from a minimum of 0.625 centipoise at the saturation pressure to a maximum of 1.704 centipoises at atmospheric pressure. The saturation pressure of the fluid was measured at several different temperatures as you requested.

It has been a pleasure to perform this study for you. If you have any questions or if we may assist you further in any way, please do not hesitate to contact us.

Very truly yours,

Core Laboratories, Inc. Reservoir Fluid Division

P.L. Moses (a)

P. L. Moses Operations Supervisor

PLM:JB:bjm 7 cc. - Addressee

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			Page10f11
	Benson-Montin-Greer		File
Company	Drill.ng Corporation	Date Sampled	July 1, 1965
Well	Canada Ojitos Unit No. 12-11	County	Rio Arriba
Field	Puer: c Chiquito		New Mexico

FORMATION CHARACTERIS	TICS	
Formation Name	<u>Nio Braro (Gal</u>	lup)
Date First Well Completed	October	, 19_62
Original Reservoir Pressure	<u>_1631</u> PSIG	@ <u></u>
Original Produced Gas-Oil Ratio		SCF/Bbl
Production Rate		Bbl/Day
Separator Pressure and Temperature	PSI(д,°F.
Oil Gravity at 60° F.		°API
Datum		Ft. Subsea
Original Gas Cap		

WELL CHARACTERIST	rics
Elevation	<u>7232 KB</u> Ft.
Total Depth	<u> 6687 </u>
Producing Interval	_6648-6687Ft.
Tubing Size and Depth	In. toFt.
Productivity Index	Bbl/D/PSI @Bbl/Day
Last Reservoir Pressure	<u>_1693</u> PSIG @6650Ft.
Date	July 1 , 19 65
Reservoir I'emp erature	<u>162</u> °F. @ <u>6650</u> Ft.
Status of Well	Shut in 27 days
Pressure Gauge	Amerada
Normal Production Rate	Bbl/Day
Gas-Oil Ratio	SCF/Bbl
Separator Pressure and Temperature	PSIG,°F.
Base Pressure	15.025 PSIA
Well Making Water	_None% Cut

SAMPLING CONDITIONS

Sampled at	_6650 KB	Ft.
Status of Well	Shut in 27 days	
Gas-Oil Ratio		SCF/Bbl
Separator Pressure and Temperature	PSIG,	°F.
Tubing Pressure	0	PSIG
Casing Pressure	_0	PSIG
Core Laboratories Engineer	NT	
Type Sampler	Perco	

REMARKS:

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File	RFL 3366	
Well	Canada Ojito	s Unit
	No. 12-11	

VOLUMETRIC DATA OF Reservoir Fluid SAMPLE

1.	Saturation pressure (bubble-point pressure) <u>1519</u> PSIG @ <u>162</u> °H	
2.	Thermal expansion of saturated oil @ 5000 PSI = $\frac{V @ 162 \circ F}{V @ 76 \circ F} = \frac{1.04528}{1.04528}$	
3. Compressibility of saturated oil @ reservoir temperature: Vol/Vol/PSI:		
	From <u>5000</u> PSI to <u>3500</u> PSI = <u>8.24 x 10^{-6</u>	
	From <u>3500</u> PSI to 2500 PSI = <u>9.49 x 10^{-6</u>	
	From 2500 PSI to 1519 PSI = 10.68×10^{-6}	
4.	Specific volume at saturation pressure: ft 3/lb	

4. Specific volume at saturation pressure: ft ³/lb

CL. 516

5. Saturation pressure at various temperatures:

Temperature,	Saturation Pressure, PSI		
• F.	BHS No. 1	BHS No. 2	
76	1203	1204	
110	1351	•	
152	1491	1492	
162	1519	1519	
172	1540		

, 22218 ++ 3/# (.02218(144) = .313 #/1n=/ f+,

CORE LABORATORIES, INC. Petroleum Reservoir Engineering

DALLAS, TEXAS

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File	RFL 3366	
Well	Canada Ojitos Unit	
	No. 12-11	_

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Reservoir Fluid SAMPLE TABULAR DATA

-		PRESSURE-VOLUME	VISCOSITY	DIFFERENTIAL LIBERATION @ 162 "F.		
	PRESSURE PSI GAUGE	@ 162 "F., RELATIVE VOLUME OF OIL AND GAS, V/VEAT.	@ 162 F., CENTIPOISES	GAS/OIL RATIO Liberated Per Barrel of Residual oil	GAS/OIL RATIO IN SOLUTION PER BARREL OF RESIDUAL OIL	RELATIVE OIL VOLUME, V/VR
SIN					••••••••••••••••••••••••••••••••••••••	
1	5000	0.9680	0.841	:		1.256
	4500	0.9718				1.260
	4000	0.9759	0.781			1.266
	3500	0.9801	0.751			1.271
	3000	0.9847	0.719			1.277
	2500	0.9895	0.686			1.283
	2300	0.9916 N.L			•	1.286
	2100	0.9936				1.289
	2000	0.9947	0.652			1.290
	1900	0.9957				1.291
	1800	0.9968				1.293
	1700	0.9981				1.294
	1600	0.9991		-		1.296
153	1519	1.0000 3/3	0.625	0	478	1.297
	1508	1.0328	-			
	1498	1.0054				
	1481	1.0101				
	1457	1.0162				
	1429	1.0254				
	1389			32	446	1.284
	<u>1369</u>	1.0458 .294	1			
	1350		0.684	•		
	1288-	1.0766 ,29	4			
	1259			65	413 :	1.270
	1250		0.696			
	1196	1.1174 .28	<u>o</u>			
	1129			96	382	1.257
	1100	•	0.731			
109	B 1084	1.1789 .26:	5			
	968	1.2610 .24	δ.			
	963			136	342	1.239
	950		0.780			
	858	1.3638 2.30	2			
	812			173	305	1.224

v = Volume at given pressure

 $v_{\text{SAT.}}$ = Volume at saturation pressure and the specified temperature.

 v_{R} = Residual oil volume at 14.7 PSI absolute and 60° F.

CORE LABORATORIES, INC.

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Petroleum Reservoir Engineering DALLAS, TEXAS

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File	RFL 3366	
Well	Canada Ojito	s Unit
	No. 12-11	

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Reservoir Fluid SAMPLE TABULAR DATA

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		PRESSURE-VOLUME	VISCOSITY	DIFFERENTIAL LIBERATION @ 162 .F.		
PRI PSI	ESSURE GAUGE	4 162 'F., RELATIVE VOLUME OF OIL AND GAS, V/VSAT.	OF OIL @ 162'F CENTIPOISES	GAS/OIL RATIO Liberated Per Barrel of Residual oil	GAS/OIL RATIO IN SOLUTION PER BARREL OF RESIDUAL OIL	RELATIVE OIL VOLUME, V/VR
	800	DENSI	TY 4 0 005			
	800		0.835			
	<u>/50</u>	<u>1.4975</u> 20	4	•••	- / -	
67Z	658	•		211	267	1.207
	65/	1.6518	<u>Y</u>			
	650		0.900			
227	500	1.8577	8	• • • •		
ورح	519			246	232	1.192
	500		0.980			
	479	2.1482/44	2_			
	413	2.4573 /2;	7			
373	359			287	191	1.175
	350	2.8694 10	9			
	298	3.3145	14	-		
	<u>250</u>	3.8813	1.161			
232	218			328	1 50	1.156
122	108			367	111	1.133
14	0		1.704	478	0	1.049
					@ 60 ⁰ F	. = 1.000

Gravity of residual oil = 38.2° API @ 60° F.

v = Volume at given pressure

 $v_{\text{ear.}}$ = Volume at saturation pressure and the specified temperature.

 v_{R} = Residual oil volume at 14.7 PSI absolute and 60° F.

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Well	Canada Ojitos Unit
	No. 12-11

Differential Pressure Depletion at 162° F.

Pressure PSIG	Oil Density Gms/Cc	Gas <u>Gravity</u>	Deviation Factor
1519	0.7223		•
1 389	0.7258	0.696	0.882
1259	0.7298	0.698	0.887
1129	0.7336	0.701	0.894
963	0.7389	0.709	0.902
812	0.7438	0.718	0.914
658	0.7487	0.731	0.929
519	0.7534	0.753	0,943
359	0.7589	0.791	0.958
218	0.7642	0.886	0.976
108	0.7716	1.067	
0	0.7939	1.702	

These analyses, opinions or interpretations are based on observations and material supplied by the client to whom, and for whose exclusive and confidential use, this report is made. The interpretations or opinions expressed represent the best judgment of Core Laboratories. Inc. (all errors and omissions exceeded): hut ÷.,

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File RFL 3366

Well Canada Ojitos Unit No. 12-11

SEPARATOR TESTS OF Reservoir Fluid SAMPLE

SEPARATOR PRESSURE, PSI GAUGE	SEPARATOR TEMPERATURE, ' F.	SEPARATOR GAS/OIL RATIO See Foot Note (1)	STOCK TANK GAS/OIL RATIO See Foot Note (1)	STOCK TANK GRAVITY, * API @ 60* F.	SHRINKAGE FACTOR, VR/VEAT. See Foot Note (2)	FORMATION VOLUME FACTOR, VSAT./VR See Foot Note (3)	SPECIFIC GRAVITY OF FLASHED GAS
0	74	483		38.1	0.7639	1.309	0.986
40	74	386	27	39.6	0.7943	1.259	
80	74	354	55	39.6	0.7968	1.255	
160	74	300	110	39.4	0.7943	1.259	

110 x 14.7 15,025 = 108 cf /601

- (1) Separator and Stock Tank Gas/Oil Ratio in cubic feet of gas @ 60° F. and 14.7 PSI absolute per barrel of stock tank oil @ 60° F.
- (2) Shrinkage Factor: Va/VEAT. is barrels of stock tank oil @ 60° F. per barrel of saturated oil @ 1519 PSI gauge and 162 ° F.
- (3) Formation Volume Factor: Var./Va is barrels of saturated oil @<u>1519</u> PSI gauge and <u>162</u>° F. per barrel of stock tank oil @ 60° F.

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	Benson-Montin-Greer		File RFL 3366
Company_	Drilling Corporation	Formation	Nio Braro (Gallup)
Well	Canada Ojitos Unit No. 12-11	County	Rio Arriba
Field	Puerto Chiquito	State	New Mexico

HYDROCARBON ANALYSIS OF <u>Reservoir Fluid</u> SAMPLE

COMPONENT	MOL PER CENT	WEIGHT PER CENT	DENSITY @ 60° F. GRAMS PER CUBIC CENTIMETER	• API @ 60* F.	NOLECULAR WEIGHT
Hydrogen Sulfide					
Carbon Dioxide	0 20	0 08			
Nitrogen	0.13	0.03			
Methane	26.36	3, 65			
Ethane	6.86	1.78			
Propane	6.19	2, 36		1	
iso-Butane	1.20	0,60			
n-Butane	4.29	Z. 15			
iso-Pentane	1.80	1.12	-		
n-Pentane	2.14	1.33			
Hexanes	4.49	3.34			
Heptanes plus	46.34	83.56	0.8474	35.3	209
	100.00	100.00			
			(Ileator	<u>-</u>	

Core Laboratories, Inc. Reservoir Fluid Division

P.L. Moses (B)

P. L. Moses Operations Supervisor

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PRESSURE: POUNDS PER SQUARE INCH GAUGE

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RELATIVE LIQUID VOLUME: V/VR

PRESSURE: POUNDS PER SQUARE INCH GAUGE

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VISCOSITY OF RESERVOIR FLUID Benson-Montin-Greer Company Drilling Corporation Nio Braro (Gallup) Formation _ Canada Ojitos Unit No. 12-11 Well Rio Arriba County_ Fuerto Cniquito New Mexico Field _ State 2.0 1.8 1.6 1.4 1.2 1.0 0.8 0.6 0.0 ā 1000 2000 3000 4000 5000 6000

PRESSURE: POUNDS PER SQUARE INCH GAUGE

V----SIT\. ----VTIF ----S
CORE LABORATORIES. INC. Petroleum Reservoir Engineering DALLAS. TEXAS

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BOULDER MANCOS

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BOULDER MANCOS

(**Oil**)

T. 28 N., R. 1 W., NMPM Rio Arriba County, New Mexico

GEOLOGY

Regional Setting: East Jank, San Juan Basin

- Surface Formations: Cretaceous, Lewis Shale; Tertiary- Cretaceous, Animas Formation; and Tertiary, San Jose Formation
- Exploration Method Leading to Discovery: Probably subsurface

Type of Trap: Fracture 1 shale on a monocline

Producing Formation: Cretaceous, Mancos Shale

Gross Thickness and Lithology of Reservoir Rocks: See field commentary

Geometry of Reservoir Rock: See field commentary

Other Significant Show :: None

Oldest Stratigraphic Horizon Penetrated: Cretaceous, Mancos Shale

DISCOVERY WELL

Name: P-M Drilling Co. No. 1 Bayless

Location: NE NE (330' FNL and 330' FEL), sec. 15, T. 28 N., R. 1 W.

Elevation (KB): 7,427 feet

Date of Completion: May 15, 1961; plugging approved in 1965

Total Depth: 4,429 feet

Production Casing: 4¹/₂ " at 4,150 feet cemented with 50 sacks of cement

Perforations: Open hole 4,150 feet to 4,429 feet

Stimulation: Sand-oil fracture with 42,000 gallons of oil and 20,000 lbs. of 20/40 sand; treating pressure 2,500 lbs. Injection rate 33 barrels per minute

Initial Potential: Pump 85 BOD

Bottom Hole Pressure: Unknown

DRILLING AND COMPLETION PRACTICES

Set 8 5/8" to 10³/4" casing at approximately 130 feet with 100 sacks of cement; drill with gel-type mud to about 600 feet above pay, set 5¹/₂" to 7¹/₂" intermediate casing with 150 sacks of cement; drill to total depth with gas or air; set 4¹/₂" liner to total depth; perforate and oil-fracture with about 60,000 gallons of oil. Variations are to set slotted liner or complete open-hole. Some natural completions have been made.

RESERVOIR DATA

Productive Area:

Proved: 1,700 acres

Unproved: North and south limits of field not defined by dry holes

Approved Spacing: 80 acres

By: C. N. Needham Mobil Oil Corporation

No. of Producing Wells: 7 No. of Abandoned Wells: 18 No. of Dry Holes: 4

Average Net Pay: Fractured reservoir; gross productive interval ranges from 51 feet to 643 feet and averages 278 feet

Porosity: Fracture porosity -

Permeability: Fracture permeability

Water Saturation: Unknown

Initial Field Pressure: Unknown

Type of Drive: Gravity, solution gas

Gas Characteristics and Analysis: Unknown

Oil Characteristics and Analysis: 37° API gravity, 0.1 percent sulfur

Original Gas, Oil, and Water Contact Datums: Variable

Estimated Primary Recovery: Has produced 1,000 barrels per acre to July 1977

Type of Secondary Recovery: None

- Estimated Ultimate Recovery: 1,700,000 BO, 1,500,000 MCFG
- Present Daily Average Production: 60 BOD, 15 MCFGD, 14 BWD
- Market Outlets: Oil, Shell Pipeline Corporation; gas, used for lease operation or vented

FIELD COMMENTARY

The Boulder field is in northwest New Mexico, about sixteen miles northeast of the town of Gavilan on State Highway 96 on the Jicarilla Indian Reservation. It is located on the east flank of the San Juan Basin.

The field is on a monocline imposed on regional west dip. No closure or nose is mapped in the area of the field. Production is from fractures in the Mancos Shale. The cause of the fractures in the San Juan Basin have been discussed by several authors who present different interpretations. The reader is referred to London (1972), and Gorham, and others (1977), for recent reports on fractured Mancos Shale production.

An analysis of a fractured reservoir such as Boulder is a singularly vexatious task because few parameters can be defined adequately. However certain observations can be made:

- 1. The field has produced 1,700,000 BO, 1,400,000 MCFG, and 700 BW since discovery. Production has ranged from a high of 465,798 BO in 1963 to a low of 16,197 BO in 1975. In July 1977, the field produced 60 BOD. The conclusion is that the field is nearly depleted using present production methods.
- Water recovery has been reported on completion of some wells: S.O.T. No. 6, SE¹/₄SW¹/₄, sec. 26, T. 28 N., R. 1 W.; S.O.T. No. 7, NW¹/₄NE¹/₄, sec. 35, T. 28 N., R. 1 W.; Gulf No. 1-298, SE¹/₄SE¹/₄, sec. 10, T. 28 N., R. 1 W.; Mobil No. 14-23, SW¹/₄SW¹/₄, sec. 12, T. 28 N., R. 1 W.; and during the completion attempt S.O.T.

No. 8 Jicarilla. SW $\frac{1}{4}$ NE $\frac{1}{4}$, sec. 15, T. 28 N., R. 1 W. During July 15.77 four wells produced water with oil. Origin of this water is unknown and may come from several zones a i different intervals are open for production in various wells (see cross-section). The connection of productive i itervals by fracture systems and possible faults seems probable in this field.

3. The field has no limiting dry holes on the north or south, and has had no wells drilled deeper than the Mancos.

Net pay, porosity, permeability, water saturation and drainage area are not known. The reader again is referred to London (1972), Gorham (1977), and others for study results of the East and Wes Puerto Chiquito fields for which more data is available. These fields are 15 to 20 miles south of Boulder, and some of the data might be applied to the Boulder field.

REFERENCES

Gorhani, F. D. Jr., Woodward, L. A., Callender, J. F., and Greer, A. R., 1977, Fracture Permeability in Cretaceous Rocks of the San Juan Basin, *in* San Juan Basin III: New Mexico Geol. Soc. Guidebook, 28th Field Conf., p. 235-241.

International Oil Scouts Assoc., Part 2, 1961-1976 incl.

Ira Rineharts Yearbook, 1962.

London, W. W., 1972, Dolomite in Flexure-Fractured Petroleum Reservoirs in New Mexico and Colorado: Am. Assoc. Petroleum Geologists Bull., v. 56, no. 4, p. 815-821.

Petroleum Information statistical reports.

N	D. OF WEL	LS@YR. E	PRODUCTION: OIL IN BARRELS GAS IN MCF									
YEAR	TYPE	PROD.	S.I./ABND	ANNUAL	CUMULATIVE							
1041	OIL	6		40,716	40,716							
1701	GAS			15,608	15,608							
1042	OIL	13	10	263,431	304,147							
1702	GAS			104,296	119,904							
1963		21	3	465,798	769,945							
	GAS	L		312,545	432,449							
1064		20	3	363,410	1,133,355							
	GAS			488,425	920,874							
1965	OIL	10	10	154,195	1,287,550							
	GAS			280,493	1,201,367							
1966	<u> </u>	12	7	70,629	1,358,179							
	GAS			98,281	1,299,648							
1967	OL	8	<u> </u>	<u>44,892</u>	1,403,071							
	GAS			40,000	1,339,648							
1968	OIL	8		33,115	1,436,186							
1708	GAS			6,968	1,346,616							
1969	OIL	9	10	35,492	1,471,678							
1709	GAS			48,311	1,394,927							
1070	OIL	9	8	64.610	1,536,288							
1970	GAS		1	20,774	1,415,701							
1071	OIL	9	8	46.444	1,582,732							
1971	GAS		1	22,880	1,438,581							
1070	OIL	9	8	29,361	1,612,093							
19/2	GAS		1	9.123	1,447,704							
1070	OL	6	1	23,475	1,635,568							
19/3	GAS	1	1	7,776	1.455,480							
	ÔL		9	25,886	1.661.454							
19/4	GAS	1	1 1	NONE REPORTED	1,455,480							
	OIL	8	9	16.197	1,677,651							
C 141	GAS	1	1 1	2.684	1,458,164							
107/	OIL	8	9	20,886	1.698.537							
14/0	GAS	1	1 i	6.868	1.465.032							
	OIL	7	10	11.022	1709.559							
1977	GAS	1	1 1	6754	1471786 10 7-1							



BOULDER MANCOS





[Four Corners Geological Society

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REFERENCES

- 1. Fr.ck, Thomas C. and Taylor, William R., Petroleum Production Haudbook, Page 37-23.
- 2. Craft and Hawkins, Applied Petroleum Reservoir Engineering , Page 368.
- 3. Muskat, Morris, <u>Physical Principles of Oil Production</u>, 1949, Page 48".
- 4. Lewis, J.O., <u>Gravity Drainage in Oil Fields</u>, Trans AIME, Volume 15%, Page 133.

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NOTES ON ANALYSIS OF PRESSURE PULSES GENERATED BY FRAC TREATMENTS IN THE FRACTURED SHALE RESERVOIR OF THE NIOBRARA MEMBER OF THE MANCOS FORMATION IN THE WEST PUERTO CHIQUITO POOL RIO ARRIBA COUNTY, NEW MEXICO

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MARCH 17, 1988

BENSON-MONTIN-GREER DRILLING CORP. EXHIBIT IN CASE NO. 9111 BEFORE THE OIL CONSERVATION COMMISSION OF THE NEW MEXICO DEPARTMENT OF ENERGY AND MINERALS

Albert R. Greer

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BENSON-MONTIN-GREER DRILLING CORP. EXHIBIT IN CASE NO. 9111 BEFORE THE OIL CONSERVATION COMMISSION OF THE NEW MEXICO DEPARTMENT OF ENERGY AND MINERALS

MARCH 17, 1988

INDEX

- SECTION A. NOTES ON ANALYSIS OF PRESSURE PULSES GENERATED BY FRAC TREATMENTS IN THE FRACTURED SHALE RESERVOIR OF THE NIOBRARA MEMBER OF THE MANCOS FORMATION IN THE WEST PUERTO CHIQUITO MANCOS POOL
 - 1. Summary and Discussion (5 pages, white)
 - 2. Plat showing area of frac pulse tests (white)
 - 3. Summary of Four Frac Pulse Tests West Puerto Chiquito (white)
- SECTION B. RESPONSE TO TYPICAL FRAC TREATMENT WEST PUERTO CHIQUITO MANCOS POOL
 - 1. Introductory page (blue)
 - 2. Graph: Response to Typical Frac (blue)
 - 3. Discussion (yellow)
 - 4. Graph: Response to Typical Frac (yellow)
 - 5. Discussion (blue)
 - 6. Statistics (blue)
 - 7. Discussion (yellow)
 - 8. Statistics (yellow)
- SECTION C. RESPONSE TO FRAC TREATMENT: CANADA OJITOS UNIT N-31
 - 1. Introductory page (white)
 - 2. Plat showing area of interference testing (white)
 - 3. Graph: Frac Response in COU E-6 of N-31 Frac (gold)
 - 4. Plat Showing Locations of Wells in the Vicinity of the OUU N-31 and OUU E-6 (gold)
 - 5. Statistics (pink)
 - 6. Graph: Response to N-31 Frac 4/1/86 (pink)
- SECTION D. RESPONSE TO FRAC TREATMENT: DUGAN TAPACITOS 4
 - 1. Introductory page (white)
 - 2. Plat showing area of interference testing (white)
 - 3. Graph: Frac Response in COU E-6 of Tapacitos 4 Frac (yellow)
 - 4. Plat Showing Locations of Wells in the Vicinity of the Dugan Tapacitos 4 and COU E-6 (yellow)
 - 5. Statistics (tan)
 - 6. Graph: Response to Tapacitos 4 Frac (tan)

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- SECTION E. RESPONSE TO FRAC TREATMENT: CANADA OUITOS UNIT F-30
 - 1. Introductory page (white)
 - 2. Plat showing area of interference testing (white)
 - 3. Graph: Response to Frac Treatment of COU F-30 9/4/86 in Bottom Hole Pressure of COU B-32 (green)
 - 4. Graph: Rate of Pressure Increase COU B-32 Sept. 3 & 4, 1986 Prior to Frac Treatment of COU F-30 (green)
 - 5. Statistics (buff)
 - 6. Graph: Response to F-30 Frac 9/4/86 (buff)
- SECTION F. RESPONSE TO FRAC TREATMENT: CANADA QUITOS UNIT C-34
 - 1. Introductory page (white)
 - 2. Plat showing area of interference testing (white)
 - 3. Statistics (green)
 - 4. Graph: Response to C-34 Frac 4/23/87 (green)
- SECTION G. RESPONSE TO FRAC TREATMENT: VARIATION OF CURVE SHAPES WITH INPUT PARAMETERS
 - 1. Introductory page (white)
 - 2. Plat Showing Locations of Wells in the Vicinity of the COU N-31 and COU E-6 Frac Treatment Interference Test (white)
 - 3. Graph: Response to N-31 Frac 4/1/86 (gold)
 - 4. Graph: Response to N-31 Frac 4/1/86 (gold)
 - 5. Graph: Response to N-31 Frac 4/1/86 (tan) 6. Graph: Response to N-31 Frac 4/1/86 (tan)

 - 7. Discussion (blue)
 - 8. Graph: Response to N-31 Frac 4/1/86 (blue)

SECTION H. REFERENCES

- 1. Index page to References and Appendices (white)
- 2. Pressure Interference Effects Within Reservoirs and Aquifers article (4 pages, blue) and Graph: Error of EI Solution as Dependent on Radius Ratio & Dimensionless Time (yellow)
- 3. John Lee, SPE Textbook Series, Vol. I, page 133 (gold)
- 4. John Lee, SPE Textbook Series, Vol. I, page 90 (green)

SECTION I. APPENDICES

- Determination of Pore Volume, øh, from Appendix I. Pressure Response to Frac Treatment Using EI Solution (by Superposition) (pink)
- Appendix II. Determination of Koh (3 pages, white) and Graph (blue)

<u>A</u>

NOTES ON ANALYSIS OF PRESSURE PULSES GENERATED BY FRAC TREATMENTS IN THE FRACTURED SHALE RESERVOIR OF THE NIOBRARA MEMBER OF THE MANCOS FORMATION IN THE WEST PUERTO CHIQUITO POOL RIO ARRIBA COUNTY, NEW MEXICO MARCH, 1988

SUMMARY

Analyses of pressure responses to four frac treatments showed an average pore volume of ϕ h of approximately .34 (equivalent to a volume of stock tank oil in place of about 2000 barrels per acre) for three of the tests in which three zones were open. In the test with only two zones open in the treated well, a value of 1100 stock tank barrels per acre was determined. These values are consistent with those derived from interference tests twenty years ago and from approximate material balance estimates.

An average value for Kh/u was about 80 darcy feet. Translated to Koh: three wells were in the range of 10 to 20 darcy feet; and one was 50 darcy feet. These values, too, are consistent with that estimated 20 years ago for the high capacity fracture system and are believed to be more representative of it than that for the total reservoir combination of high capacity fracture system and tight blocks. Some influence from the tight blocks is believed to show in the tests that covered up to four days. In all instances curve matching at later times shows lower values of Kh/u; which is believed may be the consequence of greater diffusion from the high capacity system into the tight blocks as time increases.

Of significance is the fact that the pore volumes associated with these high transmissibilities undoubtedly represent a large percent of the total pore volume. High values of Koh associated with large part of the total oil in place <u>means that gravity drainage</u> is a v.able recovery mechanism for which to strive.

Three of the tests described herein were conducted pursuant to suggestion by members of the Gavilan Engineering Committee. Results of the first two tests provided to the Engineering Committee revealed that an empirical relation appeared to exist of the frac volume, frac rate and distances between wells; suggesting that the data might be subject to analysis. However, before the Engineering Committee undertook an analysis of the subject, the Committee's work was suspended.

The enclosed analysis is hereby provided, in lieu of the otherwise joint effort of the Committee members.

DISCUSSION

In a reservoir such as the one being produced in the West Puerto Chiquito pool in which a high capacity fracture system extends over the reservoir, it is to be expected that a fracture treatment of the size typically used would create a pressure pulse in nearby (up to 2 miles) wells measureable with the sensitive pressure equipment that has become generally available in the 1980's. Further it is to be expected (intuitively) that the characteristics of the reservoir governing the behavior of the pressure pulse would be more that of the high capacity fracture system rather than that of the tight blocks; although as the length of time from the frac treatment increases, diffusion from the high capacity system into some of the tight blocks should occur. It is of interest to examine interference testing of some of the fracture treatments in an effort to add additional knowledge about the reservoir's physical properties.

A virtue of frac pulse testing as opposed to normal interference testing - particularly for areas of low capacity wells the frac pulse test can yield results in a relatively short length of time, requiring much shorter shut-in periods of wells in the vicinity, minimizing the revenue loss attendant with long shut-in periods.

The explicit analytical solution of the reservoir pressure response to a frac treatment with a long fracture in a finite reservoir appears, at best, difficult to use; particularly for analysis of the subject reservoir in which none of the physical properties, permeability, porosity or pay thickness, are individually known. However, given the large areal extent of the reservoir, the point source (exponential integral) solution should yield results accurate enough for practical interpretation of some combinations of the reservoir parameters (Kh/u and øh, John Lee reference 1).

Qualitatively, it is to be expected that the first part of a pressure pulse generated by a frac treatment will arrive earlier and in greater magnitude – than that for a similar volume injected without fracturing the formation.

Once the frac treatment has ended, however, the continuing diffusion can be expected to follow that described by the diffusivity equations; and if the fracture blocks are small compared to the overall "area of influence" of the test, the flow system will approach that of radial - and the EI solution of the diffusivity equation will yield reasonably accurate results.

Since the diffusion of the pressure pulse will follow first through the high capacity fracture system and then into the fracture blocks, it is to be further expected that analyses of the earlier part of the test will reflect more of the character of the high capacity fracture system than that of the overall average.

The two factors limiting the accuracy of the EI solution are that the reservoir is of finite size and that the induced fracture causes the pressure effects of the injected fluid to deviate from that which would obtain for a "point source".

As to the first matter, the pressure response will deviate from that for the infinite solution only when the situation is such that boundary conditions become significant; and given the dimensions of the reservoir and the distance between the treated well and the observation wells for the tests run in West Puerto Chiquito, this influence of boundary conditions probably will not be significant until times longer than those occurring in the subject tests.

Also as to the deviation brought about by the effective wellbore radius being greater than a point source, estimates of the amount of this deviation (Mueller and Witherspoon reference 2) suggest that for the conditions of these tests and for assumed effective rw's of less than 250' that the amount of this error may not be significant for the points of curve matching used herein. (Times at which the error from this source is 10% and 2% are shown on the schedules and graphs herein for each test).

From a practical analysis standpoint and the fact that given the nature of the reservoir and the high capacity fracture system, it will be impossible to determine - as can be done in some reservoirs - the length of the induced fracture. Given this uncertainty - and the small difference in the exact solution with the EI formula for the probable ranges of "effective rw" - use of the more cumbersome exact solution to the diffusivity equation for these frac pulse tests does not appear warranted.

Since pressure responses for observation wells located more than a mile from the treated well may have values of less than l#, it is necessary to use sensitive pressure measuring equipment, and to eliminate interference effects of other wells. In the instance of some of the tests in the Canada Ojitos Unit, all wells within a townsh:p were shut in to minimize the effect of interference from other wells. Here reliable data was obtained. In some of the other tests the pressure pulses were substantially greater than the interference effect of producing wells, and consequently that data is believed to be reasonably accurate.

Although either two or three zones were open during the tests [a situation less desirable than that for a single zone) it is believed that the characteristics of - or averages of - the dominant zone(s) will be reflected in the analyses.

The analysis is simply that of the pulse testing procedure, except that the information is limited to a single pulse. The nerein-recommended procedure is to calculate a series of curves, assuming for each curve a value of Kh/u and diffusivity constant. By curve matching against the field data determine directly the appropriate value of Kh/u and, indirectly (Appendix I) calculate \emptyset h.

DISCUSSION - PAGE 3

Since free gas that occurs after reservoir pressures drop below the bubble point greatly increases the overall mobility (John Lee, reference 3), and since the A and B zones appear in places to have free gas indigenous, the diffusivity constant is high - both for pressures above the bubble point and below the bubble point.

From the 1965 interference test, it was determined that - on average (combination of both the tight blocks and high capacity fracture system) - the ratio of K/ϕ was in excess of 10 darcys; and that K/ϕ , as well as Kh, for the high capacity system alone should be substartially higher. The frac pulse testing shows this to indeed be the case.

From the herein-described frac pulse tests, the curve matching showed diffusivity constants in a small range of 4×10^6 to 6×10^6 . It is believed that all of these frac pulse tests were conducted when pressure of the dominant zones was below the bubble point; and although compressibility will vary some for the different tests, for the comparative analyses shown herein, a system compressibility of 350×10^{-6} per pound was used for all tests to compute ϕ h.

Although Kh, Koh and KTh/uT (total mobility) are independent of compressibility, it is necessary to know system compressibility to determine \emptyset h. For a pressure of 1400# (internediate pressure for all of the tests) the main factor affecting compressibility is that of the saturated oil (approximately 300 x 10^{-6}). Cg is approximately 800 x 10^{-6} and Cf is estimated at 15 x 10^{-6} . For zero to 10% gas saturation the above translates to system compressibility ranging from about 315 x 10^{-6} to 365 x 10^{-6} ; so the value cf 350 x 10^{-6} should be within about 10% in all of the tests. Not knowing exactly the gas saturation, it is doubtful that more precise figures can be developed.

To convert the values of Kh/u to Koh requires information independent of the frac pulse data. Apparently all that is required is the GOR (and the viscosity of the oil and the gas along with oil and gas formation volume factors, Bo and Bg) (Appendix II).

For any given PVT values, the relation of total mobility to Koh as defined by Kg/Ko, Kro, Krg is such that it can be determined independently of the knowledge of each of these parameters. There appears to be a unique relation between KTh/ut and Koh, such that Koh car be determined from a knowledge of only total mobility and GOR (Appendix II).

Summary of test results of areas of investigation are shown on the pages next following. The areas shown on the graphs are the minimum areas of investigation (the ellipsoid shaped areas inside the "influence rectangle") depicted on the plat (John Lee, reference 4).

Individual tests are detailed in the succeeding sections.

(Technical note: because of the relatively high injection rates and the fact that the calculated pressure response is the result of differences in computed values - the consequence of superposition - it is necessary that the EI function be more accurately determined than that for typical pulse testing. The degree of accuracy required can be determined by computing the pressure if injection were continous, as shown on some of the examples herein. Generally, a value of the EI function accurate to 6 or 8 significant figures is suitable. A computer with basic precision of 14 or 16 significant figures will yield that accuracy for EI(-x) for values of x less than 10. If the computations are such that values of x exceed 10, higher precision may be required. In this respect, it is helpful to know - print-out - the values of x as shown in the examples herein.)



SUMMARY OF FOUR FRAC PULSE TESTS WEST PUERTO CHIQUITO POOL

	Well Pair	000 N-31	Tapacitos 4 ccu E 6	000 F-30 000 E-30	000 C-34 000 D-34
2]) Color of Test Area on Facing Page	red	yellow	blue	gr een
3)	Date of Treatment	4/1/86	2/13/86	9/4/86	4/23/87
5)	Zones Open Treated Well Observation Well	A, B, C A, B, C	A, B, C A, B, C	A, B, C A, B, C	A, B A, B, C
(j) 20	Approximate Area of Investigation (Influence) (Acres) at ending day ()	5100 (4)	1200 (.7)	6000 (4)	6500 (4)
66	Pore Volume, øh Pore Volume, Stock Bbls/Acre	.25 1500	.47 2800	.31 1800	19 0011
10)	Average Transmissibility, Kh/u Darcy feet/centipoise	64	125	68	48
11)	Estimated GOR (cubic feet/bbl) for Area of Influence	2000	800	1050	1200
12)	Ratio of Koh to Kh/u for GOR (graph, page 4 of Appendix II)	.19	.41	.33	.30
13)	koh (from lines ll and l2) (darcy feet	.) 12	51	22	14

In heavy black outline as noted on plat on facing page are boundaries of the 13th revision of the Canada Ojitos Unit Participating Area (area requested for inclusion in pressure maintenance project). Note:

В

RESPONSE TO TYPICAL FRAC TREATMENT WEST PUERTO CHIQUITO MANCOS POOL

Analyses of four tests in dest Puerto Chiquito showed for Kh/u a value of about 80, with a diffusivity constant of about 5 x 10 . From this intormation a family of curves was developed showing the pressure response to be anticipated at varying times for wells at varying distances from the treated well. These curves are set out on the facing page showing pressure responses in wells located from 3,000° to 10,000° from a well with a fracture treatment of 8,000 barrels of slurry pumped at a rate of 100 BPM.

The curves are based on infinite conditions.

Pressure shown on the vertical scale is the pressure change resulting from the frac treatment.

differences to .01 of a pound that it is possible to obtain information which properly analyzed will reflect properties of the reservoir. Of particular significance is the fact that although the As can be seen from these typical curves, there is enough "character" to the curves and pressure differential that with pressure measuring equipment capable of measuring pressure pumping time for the typical frac treatment is only a small portion of a day (1-1/2 hours) the "pressure pulse" spreads out in time as the distance increases from the treated well.

For distances of 8,000 to 10,000 feet, the pressure is still rising after 4 days.



RESPONSE TO TYPICAL FRAC TREATMENT WEST PUERIO CHIQUITO MANCOS POOL

On the facing page are the same curves as those preceding with the time scale expanded out to 9 days.

Here it can be seen that the pressure difference at 9 days is drawing together for observation wells at varying distances from the treated well.



RESPONSE TO TYPICAL FRAC TREATMENT WEST PUERTO CHIQUITO MANCOS POOL

On the opposite page is a print-out of some of the statistics of interest in the computations. The exponential integral solution is not exact at time periods in which nt/rw² is less than 100.

This For a well with an induced fracture, the effective rw will approximate 1/4 of the fracture length from tip to tip; which for a 1000' fracture would be an effective rw of 250'. value (nt/rw^2) is determined for rw's of 1, 10, 100 and 250 feet for each calculated point.

If this value is less than 100, then the amount of difference of the EI solution from the exact solution can be approximated from the value of nt/r^2 as shown in the last column of the statistics and comparing it with the graph on page 473 of reference 2, or expanded graph, reference 2 (yellow color). For the tests herein for effective rw's of 250' (induced fracture lengths of 1000') the schedules and the graphs. At times earlier than those shown by this highlighting, the curves would time at which the error reduces to 10%, and again at 2%, is shown by highlighting on both the be expected not to match. THE COMPUTATION OF PRESSURE RESPONSE TO FRAC TREATHENT

 $(n)(t)/(r^{2})$ 0.0311 0.0887 0.1422 0.1878 0.25833 0.25833 0.3544 0.4766 0.4756 0.6978 0.6978 0.6978 0.6978 0.6978 0.9564 1.1422 1.1422 1.0311 1.1422 1.0364 1.6978 3.3568 3.3568 3.3200 ти = 250 if (n)(t)/(rw)² greater than or equal to 999 then it prints 999 111778 117738 117738 117738 117238 117238 117238 117238 117238 117238 117238 117238 117238 117238 117238 117238 117738 rw = 100 3 $(n)(t)/(rw)^{2}$ 666 666 666 rw = 0 IF X > 20 THEN EI(-X) = . -666 H MJ 1 1 dc=diffusivity constant =6.328K/((a)(c)(u)) a=porosity fraction c=compressibility u=viscosity,cp VALUE OF X IN EI FUNCTION 8.036 2.885 1.758 1.264 0.987 0.809 0.686 0.595 0.526 0.471 0.289 0.272 0.272 0.276 0.276 0.219 0.176 0.177 0.127 0.426 0.389 0.358 0.332 0.309 0.089 0.089 0.074 0.064 BFPD 0.050 056 100 144000 PRESSURE AT r IF CONTINUOUS PUMPING (PSI) 81 11
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 0.005 Pump Rate Bbls of Fluid/Minute q (Bbls of Fluid/Day) 3000 5000000 .056 BO FILE155 .058 Kh/u (Darcy ft/cp) is ۳.» 5 10 c PRESSURE RESPONSE TO FRAC AT r (PSI) ŋ 80 0 9 8 10 0 -10 -Injection Time (Days) Increment of dt (1) Ending day of dt (1) Increment of dt (2) Ending day of dt (2) <u>_</u> Output File name is .00 **Beginning Pressure** FVF ft dc Ending day of dt Increment of dt Day Shut In 5 £ Value of Val VALUE OF of TIME SINCE FRAC START (DAYS) Value 111 <u>effefefefe</u> THE The I

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RESPONSE TO TYPICAL FRAC TREATMENT WEST PUERTO CHIQUITO MANOOS POOL

Here attention is called to the computation for an observation well located 10,000' from the treated well and the fact that the pressure response (second column) increases up to a period of six days and then commences a very slow decrease.

THE COMPUTATION OF PRESSURE RESPONSE TO FRAC TREATMENT (EI SOLUTION BY SUPERPOSITION)

 $(n)(t)/(r^{2})$ 0.0178 0.0178 0.0228 0.0228 0.0478 0.0578 0.0578 0.0578 0.0578 0.0578 0.0578 0.0578 0.0578 0.0578 0.0578 0.0578 0.0578 0.0578 0.0578 0.0578 0.0578 0.0528 0.0528 0.0528 0.0528 0.1578 0.1578 0.1578 0.1578 0.1578 0.1578 0.1578 0.1578 0.1578 0.1578 0.1578 0.1578 0.1578 0.1578 0.05780 0.057888 0.0578880 .0028 0 o т**ы** = 250 1f (h)(t)/(rw)² greater than
or equal to 999 then it prints 999 28 8 $(n)(t)/(rw)^{2}$ Ł 6666 6666 6666 rw ... 999 0 11 20 THEN EI(-X) 0 dc=diffusivity constant =6.328K/((a)(c)(u)) 3-1 a=porosity,fraction c=compressibility u=viscosity, cp VALUE OF X FUNCTION IN EI 32.051 19.531 14.045 10.965 3.434 3.213 3.019 2.694 2.694 2.656 2.432 1.956 1.636 144000 BFPD 8.993 7.622 6.614 89.286 5.230 4.735 4.325 3.981 0.826 0.709 0.621 233 5.841 687 1.406 552 × 11 100 PRESSURE AT r IF CONTINUOUS PUMPING (PSI) 11 11 0.000 0.000 0.000 0.000 0.000 0.002 0.023 0.055 2.941 3.465 6.606 10.409 14.638 14.638 13.123 28.412 28.412 37.704 46.744 46.744 OF Pump Rate Bbls of Fluid/Minute OF q (Bbls of Fluid/Day) 0.113 0.199 0.325 0.492 0.703 0.703 1.267 1.267 2.962 2.941 2.941 705 1111 6000000 80 FILE159 10000 .058 .056 1.5 <u>،</u> 2 ю, 0 PRESSURE RESPONSE. TO FRAC AT r (PSI) Kh/u (Darcy ft/cp) 10 80 80 80 5 n 10 10 80 80 • 10 10 Increment of dt (1)
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Finding day of dt (2)
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RESPONSE TO FRAC TREATMENT

Treated well: Canada Ojitos Unit N-31 (Sec. 31, T-26N, R-IW) Observation well: Canada Ojitos Unit E-6 (Sec. 6, T-25N, R-IW)

Date: April 1, 1986

See plat on facing page.

Test Summary of Area and Pore Space:

Area of Investigation at 4 days: approximately 5,000 acres Pore space, ϕh = .25 or 1500 stock tank barrels per acre. A, B and C zones open.



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THE COMPUTATION OF PRESSURE RESPONSE TO FRAC TREATMENT (EI SOLUTION BY SUPERPOSITION)

dc=diffusivity constant =6.328K/((a)(c)(u)) a=porosity,fraction c=compressibility 111 159840 BFPD 11 11 THE VALUE-OF Pump Rate Bbls of Fluid/Minute THE VALUE OF q (Bbls of Fluid/Day) 55 4000000 1s 0 1s FILE146 .0468 .0468 1 2858 The Value of Kh/u (Darcy ft/cp) is .1 9. 10 5 10 13 2 15 S 13 5 13 S 5 n Increment of dt (2)
n Ending day of dt (2)
n Increment of dt (3)
n Ending day of dt (3) Injection Time (Days) Increment of dt (1) Ending day of dt (1) Beginning Pressure Output File name is FVF ft dc Increment of dt -Day Shut In B Value of n ы Value of Value of The The The The The The The The

IF X > 20 THEN EI(-X) = 0 u=viscosity, cp

n nts 999	$r_{W} = (n)(t)/(r^{2}$	3 0.0229	9 0.0719	16 0.1209	22 0.1698	29 0.2188	35 0.2678	41 0.3167	48 0.3657	54 0.4147	61 0.4637	67 0.5126	73 0.5616	80 0.6106	86 0.6595	93 0.7085	99 0.7575	105 0.8064	112 0.8554	118 0.9044	125 0.9534		131 1.0023	131 1.0023 163 1.2472	131 1.0023 163 1.2472 195 1.4920	131 1.0023 163 1.2472 195 1.4920 227 1.7369	131 1.0023 163 1.2472 195 1.4920 227 1.7369 259 1.9817	131 1.0023 163 1.0023 195 1.2472 227 1.4920 259 1.9817 323 2.4714	131 1.0023 163 1.0023 195 1.472 227 1.4920 229 1.4914 323 2.4714 387 2.9612	131 1.0023 163 1.0023 195 1.2472 227 1.4920 227 1.4364 229 1.4944 323 2.4714 323 2.9612 367 3.4509 451 3.4509
reater tha nen it pri	/(rw) ² rw = 100	19	69	88	139	179	219	259	299	339	379	419	459	499	539	579	619	629	669	739	779	819		999	666 666	666 666	666 666 666	666 666 666 666	666 666 666 666	0 0
t)/(rw) ² gi l to 999 th	rw = rw = 10	666	666	666	666	999	666	666	666	666	999	666	• 999	666	666	999	666	666	999	666	999	666		999	999	8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8	666 666 666	666 666 666 666	5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5
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	VALUE OF X IN EI FUNCTION	10.908	3.478	2.069	1.472	1.143	0.934	0.789	0.684	0.603	0.539	0.488	0.445	0.409	0.379	0.353	0.330	0.310	0.292	0.276	0,262	0.249	0.200		0.168	0.168 0.144	0.168 0.144 0.126	0.168 0.144 0.126 0.101	0.168 0.144 0.126 0.101 0.084	0.168 0.144 0.126 0.101 0.084 0.072
	PRESSURE AT r IF CONTINUOUS PUMPING (PSI)	0.000	1.471	9.132	21.401	35,631	50.389	64.997	79.149	92.720	105.672	118.011	129.761	140.956	151.634	161,831	171.581	180.919	189.873	198.471	206,739	214.700	250.556		281.180	281.180 307.877	281.180 307.877 331.530	281.180 307.877 331.530 372.003	281.180 307.877 331.530 372.003 405.826	281.180 307.877 331.530 372.003 405.826 434.872
	PRESSURE RESPONSE TO FRAC AT r (PSI)	0.00	1.26	4.36	6.12	6.79	6.92	6.79	6.56	6.28	5.98	5.70	5.43	5.17	4.94	4.71	4.51	4.32	4.14	3.98	3.83	3.69	3.11	00 0	· 00 · 7	2.36	2.36 2.10	2.36 2.10 1.73	2.36 2.10 1.73 1.47	2.36 2.10 1.73 1.27
	TIME SINCE FRAC START (DAYS)	0.05	0.15	0.25	0.35	0.45	. 0.55	0.65	0.75	0.85	0.95	1.05	1.15	1.25	1.35	1.45	1.55	1.65	1.75	1.85	1.95	2.05	2.55	3 05	>> ->	3.55	3.55 4.05	3.55 4.05 5.05	3.55 5.05 6.05	3.55 5.05 6.05 7.05



RESPONSE TO N-31 FRAC 4/1/86

RESPONSE TO FRAC TREATMENT

Treated well: Dugan Tapacitos 4 (Sec. 31, T-26N, R-2W)

Observation well: Canada Ojitos Unit E-6 (Sec. 6, T-25N, R-JW)

Date: February 13, 1986

See plat on facing page.

Because of the relatively short observation time (.7 day) and small pressure differential of .6#, the calculated pore space, β h, is probably not as definitive of average reservoir conditions as for some of the other tests, although it may more accurately reflect the properties of the high capacity $^{\prime}$ system.

Test Summary of Area and Pore Space:

Area of Investigation at .7 days: approximately 1,200 acres. Pore space, $\not = .47$ or 2800 stock tank barrels per acre. A, B and C zones open.



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THE COMPUTATION OF PRESSURE RESPONSE TO FRAC TREATMENT (EI SOLUTION BY SUPERPOSITION)

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dc=diffusivity constant 70 100800 BFPD 11 11 THE VALUE OF Pump Rate Bbls of Fluid/Minute THE VALUE OF q (Bbls of Fluid/Day) The Value of Kh/u (Darcy ft/cp) is 125 4500000 1s .028 1s 0 1s FILE185 3848 .028 .03 .04 5 83 83 5 5 0 5 53 13 8 (Days 332255 Day Shut In Beginning Pressure Output File name is The Value of r (ft The Value of n (dc The Injection Time (Da The Increment of dt (The Ending day of dt (The Beginning Pressure The Output File name i (FVF Value of B The

a=porosity,fraction
c=compressibility
u=viscosity,cp =6.328K/((a)(c)(u))

0 IF X > 20 THEN EI(-X) =

	(n)(t)/(r ²)	0.0085	0.0176	0.0267	0.0359	0.0450	0.0541	0.0632	0.0723	0.0814	0.0906	0.0997	0.1118	0.1240	0.1362	0.1483	0.1605	0.1726	0.1848	0.1969	0.2091	0.2212	0.2334	0.2456	0.2577	0.2699	0.2820	0.2942
n nts 999	rw = 250	8	4	9	8	11	13	15	17	19	21	24	26	29	32	35	38	41	44	47	50	52	65	58	61	64	67	70
reater tha hen it pri	/(rw) ² rw = 100	13	26	40	53	67	80	94	107	121	134	148	166	184	202	220	238	256	274	292	310	328	346	364	382	400	418	436
t)/(rw) ² g l to 999 t	(n)(t) rw = 10	666	666	666	666	999	666	666	666	666	999	666	666	666	666	999	666	666	666	666	999	999	666	666	666	999	999	666
If (n)(or equa.	rw = 1	999	666	666	666	999	666	666	666	666	999	. 999	666	666	666	999	999	666	666	666	999	999	666	666	666	999	666	666
	VALUE OF X IN EI FUNCTION	29.379	14.183	9.348	6.971	5.558	4.621.	3.955	3.456 *	3.069	2.760	2.508	2.235	2.016	1.836	1.686	1.558	1.448	1.353	1.269	1.196	1.130	1.071	1.018	0.970	0.926	0.886	0.850
	PRESSURE AT r IF CONTINUOUS PUMPING (PSI)	0.000	0.000	0.000	0.007	0.034	0.102	0.227	0.419	0.680	1.010	1.404	2.019	2.723	3.501	4.340	5.228	6.154	7.110	8.088	9.083	10.090	11.104	12.121	13.140	14.157	15.171	16.180
	PRESSURE RESPONSE TO FRAC AT r (PSI)	0.00	0.00	0.00	0.01	0.03	0.07	0.12	0.18	0.25	0.31	0.37	0.44	0.50	0.65	0.59	0.63	0.65	0.67	0.69	0.70	0.71	0.71	0.71	0.71	0.71	0.71	0.71
	TIME SINCE FRAC START (DAYS)	0.03	0.06 .	0.09	0.12	0.15	0.18	0.21	0.24	0.27	0,30	0,33	0.37	0.41	0.45	0.49	0.53	0.57	0.61	0.65	0.69	0.73	0.77	0.81	0.85	0.89	0.93	0.97



RESPONSE TO TAPACITOS 4 FRAC

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RESPONSE TO FRAC TREATMENT

Treated well: Canada Ojitos Unit F-30 (Sec. 30. P-25N. R-1W)

Observation well: Canada Ojitos Unit B-32 (Sec. 32, T-25N, R-LW)

Date: September 4, 1986

On the facing page is a plat showing the location of the treated well F-30 and the observation well B-32. Also in the same test, interference was measured in the Meridian Hill Federal 2-Y well. Other wells were producing in the vicinity of the Hill 2-Y, however, so that its pressure response was affected, and it is believed that data for this well would not be suitable for analysis.

Test Summary of Area and Pore Space:

Area of Investigation at 4 days: approximately 6,000 acres. Pore space, $\emptyset h$ = .31 or 1,800 stock tank barrels per acre. A, B and C zones open.







THE COMPUTATION OF FRESSURE RESPONSE TO FRAC TREATMENT (EI SOLUTION BY SUPERPOSITION)

.

= 107.5 = 154800 BFPD	<pre>dc=diffusivity constant' =6.328K/(fa)(c)(n))</pre>	a=porosity, fraction	c=compressibility u=viscosity, cp	TE V > 90 THEN EI(-V)	V THE MAINI OF V AT								If (n
s of Fluid/Minute Fluid/Day)	t/cp) is 68	1s 1 1- 7000	15 4000000	1s .054	15 2	1s . 5	1s 4	is 1	1s 10	1s .054	1s 0	1s FILE144	
VALUE OF Pump Rate Bbl VALUE OF q (Bbls of F	Value of Kh/u (Darcy f	Value of B (FVF)	Value of n (dc)	Injection Time (Days)	Ending day of dt (1)	Increment of dt (2)	Ending day of dt (2)	Increment of dt (3)	Ending day of dt (3)	Day Shut In	Beginning Pressure	Output File name is	
THE	The	The	The	The	The	The	The	The	The	The	The	The	

20 THEN EI(-X) = 0

If $(n)(t)/(rw)^2$ greater than or equal to 999 then it prints 999

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HESPONSE TO F-30 FRAC 9/4/86

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RESPONSE TO FRAC TREATMENT

Treated well: Canada Oiitos Unit C-34 (Sec. 34, T-25N, R-1W) Observation well: Canada Ojitos Unit B-32 (Sec. 32, T-25N, R-1W) Date: April 23, 1987

See plat on facing page.

Test Summary of Area and Pore Space:

Area of Investigation: approximately 6,500 acres. Pore space, øh = .19 or 1,100 stock tank barrels per acre. A and B zones open in treated well. . .



THE COMPUTATION OF PRESSURE RESPONSE TO FRAC TREATMENT (EI SOLUTION BY SUPERPOSITION)

= 66 = 95040 BFPD	<pre>dc=diffusivity constant = d 328K//(=)/(.))</pre>	a=porosity (faction	u=viscosity, cp		IF $X > 20$ THEN EI(-X) = 0									If (n)(t)/(r	· or equal to f
finute	-		-												
Fluid/	1s 40	1	4000000	.071	.1	2	. 5	4	1	10	.071	0	FILE175		
ls of Fluid,	ft/cp	5	13	13	13	ls	13	15	18	15	ls	1 s	13 1		
Pump Rate Bb q (Bbls of	Kh/u (Darcy	B (FVF)	n (dc)	Time (Days)	of dt (1)	y of dt (1)	of dt (2)	y of dt (2)	of dt (3)	v of dt (3)	In	Pressure	le name is		
OF	of	of	of	lon	nent	da,	lent	da,	lent	day	ut	ing	F1		
VALUE VALUE	Value	Value	Value	Inject	Increm	Ending	Increm	Ending	Increm	Ending	Day Sh	Beginn	Output		
THE	The	The	The	The	The	The	The	The	The	The	The	The	The		

		(n)(t)/(r ²)	0.0026	0.0063	0.0100	0.0137	0.0174	0.0211	0.0248	0.0285	0.0321	0.0358	0.0395	0.0432	0.0469	0.0506	0.0543	0.0580	0.0617	0.0654	0.0690	0.0727	0.0764	0.0949	0.1133	0.1318	0.1502	0.1871	0.2240	0.2609	0.2979	0.3348
ts 999		rw = 250	2	11	17	24	30	37	43	49	56	62	69	75	81	88	94	101	107	113	120	126	133	165	197	229	261	325	389	453	517	581
reater thar hen it prir	/(rw)2	rw = 100	28	68	108	148	188	228	268	308	348	388	428	468	508	548	588	628	668	708	748	788	828	999	666	999	999	666	666	666	666	999
c)/(rw) ² g t to 999 t	(n)(t)	rw = 10	866	999	999	666	999	666	666	666	666	999	666	• 999	666	666	999	666	666	666	666	999	666	666	666	999	666	666	666	666	666	999
If (n)(t or equal		rw = 1	999	666	999	666	999	999	866	666	666	999	666	666	666	666	999	666	999	666	666	999	666	666	666	999	999	666	666	. 999	999	999
	VALUE OF X	IN EI FUNCTION	95.413	39.616	24.997	18.260	14.383	11.864 1	10.096	8.786	7.778	6.977	6.325	5.785	5.330	4.941	4.605	4.312	4.054	3.825	3.621	3.437	3.271	2.635	2.206	1.897	1.664	1.336	1.116	0.958	0.839	0.747
	PRESSURE AT r	IF CONTINUOUS PUMPING (PSI)	0.000	0.000	0.000	0.000	0.000	0.000	0.001	0.003	0.008	0.020	0.042	0.077	0.131	0.206	0.307	0.435	0.594	0.784	1.008	1.265	1.555	3.503	6.191	9.470	13.194	21.505	30.416	39.515	48.568	57.446
	PRESSURE RESPONSE	TO FRAC AT r (PSI)	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.01	0.02	0.03	0.04	0.06	0.07	0.09	0.12	0.14	0.16	0.19	0.21	0.32	0.42	0.50	0.55	0.62	0.64	0.65	0.64	0.62
	TIME SINCE	FRAC START (DAYS)	0.07	0.17	0.27	0.37	0.47	0.57	0.67	0.77	0.87	0.97	1.07	1.17	1.27	1.37	1.47	1.67	1.67	1.77	1.87	1.97	2.07	1.9.2	10.6	1.0.6	4.07	5.07	6.07	1.07	8.07	8.01

APPROXIMATE AREA OF INFLUENCE FOR n = 4E6 6.5 4 5.1 由 3 3.6 2 Area (M acres) Time (days) 1 - \$h = 6:325 × 55 = 20 PORE SPACE FOR CT = 350 X10-6 1 - \$h = 6,328 x 40 - 2 - 18 Time after frac. days U × B × × A Kh/u = 32, (FILE B32C34) A Kh/u = 32, n = 366 (FILE 175) A × × Observation well Treated well Zones open: 四 * * 9 * 0 Pressure, psi

RESPONSE TO C-34 FRAC 4/23/87

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RESPONSE 'TO FRAC TREATMENT

VARIATION OF CURVE SHAPES WITH INPUT PARAMETERS

It is of interest to compare curve sinces for different values of kh/u. If, for the value of kh/u is substantially less than for that in which the curves have been matched, the extreme difference in character is apparent by comparing the curves on the same plot. instance,

On the following pages a comparison is made with the data for the Canada Ojitos Unit N-31 and Canada Ojitos Unit E-6 frac showing the matched curves and curve which would result if Kh/u is I darcy foot and the curve matching is attempted by either matching the peak pressure and letting the data determine the time of the response (the following two gold colored pages) or matching time of the response and letting the data determine the peak pressures (next following tan colored pages). PLAT SHOWING LOCATIONS OF WELLS IN THE VICINITY OF THE CANADA OJITOS UNIT N-31 AND FRAC TREATMENT INTERFERENCE TEST



10/85



20 -19 2) MATCH PEAK PRESSORE 3) DETERVINE N= 7EH and carrie SHAPE 9. = / time it 35 9 Time after frac, days 52 J. S. ET 20. **.** 9 10 6 9 Ľ Pressure. 5 ī sd

X RPU =-6. (FILE COUNDADLE 172) RESPONSE TO N-31 FRAC 4/1/86



5 73 OBSERVED PRESSAR (A TTO of RESULTIVE MERSON OF PLAK PRESSAE 660# 000 DEXK I/JOO DETERNUE M= 7E6 2) MATCH TIME OF AT , 3 DAG 11.3 Time after frac. days () St-1- (1) m X COU E-6 (FILE COUNSI) A Kh/u = 1, n = 766 (FILE 173) 009 tsd 008 005 002 Pressure, Pressure, 007 00E 500 003 0007 Ö

HESPONSE TO N-31 FRAC 4/1/86

COMPARISON WITH RESERVOIR IN WHICH ONLY 1/10 OF PORE SPACE IS IN HIGH CAPACITY FRACTORE SYSTEM

Since the response to a frac treatment should, at early times, be more dependent upon the physical properties of the high capacity fracture system rather than the tight blocks, it is of interest to compare observed data with that which would result for a given proportion of fracture volume to total reservoir volume. In the example on the facing page, total reservoir pore space, ϕ h, is equal to .3. If the pore space of the fractures is 10% of the total, then the fracture pore space would be ϕ h equals .03. The comparison is made against the Canada Ojitos Unit N-31/Canada Ojitos Unit E-6 frac treatment of April 1, 1986 and assuming a total compressibility of 350 x 10⁻⁶.

To match peak pressures at the field data point at .3 day requires a diffusivity constant of 7×10^6 .

The resulting value for Kh/y is then 12 darcy feet; and the resulting pressure versus time curve for Kh/u = 12 and $n = 7 \times 10^{\circ}$ is shown on the facing page in which the assumed data fails by a factor of about 8 to 1 to match the observed pressures.

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10% of RESERVER UDUNE IN FRANKES 3) UETERIME PEAK PRESSURE = 55-4 (ABOUT & TIMES OBSERVED PRESSURE) X 2) THEN Kh / a 12 dary feet PEAK PRESSURE AT , 3 UAY × 1) SET dh= ,03 and MEON and E. = hay grantersed -THEN Jh (Fractures) = .03 X x x X X and Time after frac, days N 100 οZ 06 08 09 Pressure. 50 40 oε so 10 0 ī sd

X GOU E-6 2 FILE COUND 1 FILE 174) RESPONSE TO N-31 FRAC 4/1/86

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- 1. John Lee private communication.
- 2. "Pressure Interference Effects Within Reservoirs and Aquifers", Thomas D. Mueller and Paul A. Witherspoon, AIME Transactions, Volume 234 (1965), pages 471-474 (blue color, next following). and Graph "Error of EI Solution as Dependent on Radius Ratio & Dimensionless Time" (reproduction of Mueller's graph, page 473) (yellow color).
- 3. John Lee, SPE Textbook Series, Volume I, page 133 (gold color).
- 4. John Lee, SPE Textbook Series, Volume I, page 90 (green color).
- Appendix II: Determination of Koh (3 pages, white). and graph (blue color).

Pressure Interference Effects Within Reservoirs and Aquifers

THOMAS D. MUELLER PAUL A. WITHERSPOON MEMBERS AIME

ABSTRACT

For the case of an infinite radial system operating at constant terminal rate, the reservoir engineer often uses the "point source" solution of the diffusivity equation to study pressure interference effects. At early times and at short distances from the inner boundary these solutions are invalid. The amount of error is often not precisely defined because of nathematical difficulties. Work presented here shows that, if dimensionless time is defined appropriately, previous solutions of the pressure equation can be displayed as a family of curves on one chart. These solutions include the point source solution (referred to in the field of hydrology as the Theis solution) and other solutions obtained with digital computer methods. With these curves, an exact evaluation of the pressure drop within a reservoir or an aquifer can be made by the engineer. Examples of field problem solutions are presented. In most reservoirs the error involved when the Theis solution is employed is often negligible; whereas, in the calculation of interference effects in an aquifer, a substantial error can occur through such an approach.

INTRODUCTION

Flow equations are used in petroleum engineering to study the behavior of individual wells and reservoirs. In the case of wells, the pressure response at the wellbore face is the major point of interest; whereas, in the case of reservoirs, the pressure response at the interface of the aquifer boundary is sought. To aid in such studies, the flow equations have been solved in terms of the behavior at these two inner boundaries.

Only limited work has been published in regard to the pressure conditions away from these points, i.e., within the reservoir or aquifer. Theis' and Mortada' are among the few who have reported on this problem. The Theis approach employs the exponential integral and is valid for pressure conditions that occur some distance away from the flow disturbance. It is derived from the concept of a point source, as opposed to a flow across some finite area. The Mortada results, on the other hand, are valid at all points with n the reservoir or aquifer. They are presented in terms of dimensionless ratios of the radius where the pressure is desired to the radius where the flow rate is measured. Their main use, in the past, has been in aquifer studies. The published results are presented in the form of graphs that are limited to a maximum radius ratio STANDARD OIL CO. OF CALIFORNIA SAN FRANCISCO, CALIF. U. OF CALIFORNIA BERKELEY, CALIF.

of 64. These graphical results are cumbersome to interpolate at non-integral radius ratios, so that one may be forced to utilize a rather involved analytical expression presented by Mortada.

BASIC EQUATIONS

The solutions of Mortada and Theis are both based on the diffusivity equation as applied to the case of an infinite radial system subject to a constant terminal rate. The equation is obtained by combining the material balance equation with Darcy's flow equation. The assumptions implicit in the use of this equation are as follows: (1) a single fluid is present that occupies the entire pore volume; (2) the reservoir is horizontal, homogeneous, uniform in thickness, and of infinite radial extent; (3) compressibility and viscosity of the fluid remain constant at all pressures; and (4) fluid density obeys the equation

$$\rho = \rho_{\bullet} \exp(-c(p_{\bullet} - p)) \quad . \quad . \quad . \quad . \quad . \quad (1)$$

• Using the diffusivity equation in situations where the above conditions do not hold will result in errors. These errors (not discussed here) but only the errors which arise in the solution of the equation itself.

The diffusivity equation for the homogeneous reservoir conditions cited above can be written in cylindrical coordinates, as

$$\frac{\partial^2 p}{\partial r^2} + \frac{1}{r} \frac{\partial p}{\partial r} = \frac{\phi \mu c}{k} \frac{\partial p}{\partial t}. \qquad (2)$$

To obtain a dimensionless equation, so a single solution can be used for applications of different porosity, permeability and fluid properties, the following transformations are usually made:

$$p_p = \frac{2\pi k h(p_1 - p_1)}{q\mu} , \qquad (3)$$

$$r_{\nu} = r/r_{\omega} \quad , \quad \ldots \quad \ldots \quad \ldots \quad (4)$$

After these transformations are made, Eq. 3 can be written in dimensionless form, as

MORTADA SOLUTION

One solution of Eq. 6 has been given by Mortada,^a

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¹References given at end of paper.

where he presented dimensionless pressure drop as a function of dimensionless time. His graphical results are reproduced in Fig. 1. The dimensionless time is given in terms of the radius at the inner boundary, i.e., the wellbore or the aquifer boundary. Results of the dimensionless pressure crop vs dimensionless time are given at the following radius ratios: 1, 2, 4, 8, 16, 32 and 64, although results at much higher ratios are available from Mortada. As will be shown there is no need to carry out such determinations for radius ratios above 20.

van Everdingen and Hurst' have also presented results of the dimensionless pressure drop at the wellbore interface $(r_p = 1)$ as a function of dimensionless time defined in the same nanner as above. Their results correspond to Mortada results at the same $r_p = 1$. More recently, Driscoll has also used the concept of dimensionless pressure vs dimensionless time at various radius ratios.⁴

THEIS SOLUTION

The mathematical formulation of the point source solution and its resultant exponential integral are due to Lord Kelvin.^{3,3} Theis, however, is the first, to our knowledge, to demonstrate how the point source solution could be employed in the analysis of non-steady-state flow problems.¹ In recognition of his early work, the exponential integral solution is normally referred to in the field of hydrology as the Theis solution, and that term is adopted here.

In this solution, the variable X is defined as a dimensionless quantity inversely related to time. X is the independent variable in the Theis solution, and the integral value or dependent variable is related to the dimensionless pressure drop. The definitions of the dependent and independent variables are compared with those of Mortada and van Everdingen and Hurst in Table 1. The Theis solution of the exponential integral is shown in Fig. 2.

If we alter the definition of dimensionless time given in Eq. 5 to be based on any radius in the infinite system, we then have

$$t_t = \frac{kt}{\phi \mu c r^2} \qquad (7)$$

The dimensionless time of Mortada is related to that of Eq. 7, by



FI: 1-MORTADA'S POINT SOURCE SOLUTION.

TABLE 1-COMPARISON OF DEPENDENT AND INDEPENDENT VARIABLES

	Dimensionless Independent Variable	Dimensioniess Dependent Variable	Dimensioned Pressure Drop
Theis	$X = \frac{r^2 \phi \mu c}{Akt}$	Ei(-X)	$\frac{q\mu}{4\pi kh} Ei(-X)$
Mortada, and van Everdingen and Hurst	$t_D = \frac{kt}{\phi\mu cr e^2}$	مد م	<u>αμ</u> Δρ 2πkh D

$$t_{o}$$
 (Eq. 7) = $\frac{t_{o}$ (Mortada) (8)

From Table 1, it can also be seen that, with reference to the Theis solution,

and

Fig. 3 represents the Theis results of Fig. 1 with the definitions of dimensionless time and dimensionless pressure as given in Eqs. 9 and 10, respectively. By adjusting the dimensionless time of the Mortada solutions in accordance with Eq. 8, it is apparent that the array of curves on Fig. 1 becomes a family of curves on Fig. 3 that converge on the Theis solution. Other radius ratios not given in Mortada's work were obtained from the digital calculations performed to obtain the results given by Mueiler.⁵

It can be seen on Fig. 3 that, for all radius ratios greater than 20, the Theis solution adequately gives the pressure drop after any practical time.

This can be further demonstrated by the results presented in Fig. 4, which shows the relationship between the per cent error one would get in using the Theis solution for various radius ratios in place of the exact solution. It will be seen that, after a dimensionless time of 50, the Theis solution can be used with an error of only 1 per cent for all radius ratios. This, of course, is also evident from the convergence of all curves onto essentially a single line on Fig. 3. Any combination of radius ratio and dimensionless time that falls to the right of the 1 per cent line on Fig. 4 will have an error of less than 1 per cent. Correspondingly, any combination falling to the right of the 0.1 per cent line will have an error of less than 0.1 per cent.



FIG. 2-THEIS' SOLUTION OF EXPONENTIAL INTEGRAL.

NUMERICAL EXAMPLES

EXAMPLE A

To demonstrate the use of Figs. 3 and 4, let us con-

sider the following situation. We wish to know the pressure drop in an aquifer at a point that is 50,000 ft away from the center of a reservoir having an equivalent radius





FIG. 4-RELATIONSHIP FOR USING THE THEIS SOLUTION FOR VARIOUS RADIUS RATIOS INSTEAD OF THE EXACT SOLUTION.

of 5,000 ft. The aquifer and associated water have the following propert es:

$$k = 356 \text{ md, or } 2 \text{ perms}$$

$$1 \text{ perm} = 1 \text{ cu ft} - \frac{cp}{day-ft-psi}$$

$$\phi = 0.2 \text{ per cent}$$

$$c = 4 \times 10^{-4} \text{ psi}^{-1}$$

$$\mu = 1 \text{ cp.}$$

From these properties, the dimensionless time can be found from Eq. 7:

$$t_{p} = \frac{k!}{\phi \mu cr^{2}} = \frac{2t}{0.2 \times 1 \times 4 \times 10^{-4} \times 50,000^{-5}}$$

$$t_{p} = 0.0011 t$$

After 100 days, $t_0 = 0.1$, for which $\Delta p_0 = 0.0165$ at $r_0 = 10$. Fig. 4 shows that an error of about 50 per cent would result if the Theis solution were used instead of the exact solution.

To translate his into more meaningful terms, assume that h = 56.2 it and q = 1,256 B/D. From Eq. 3, we find,

$$\Delta p = \frac{q_{1} \Delta p_{p}}{2\pi kh} = \frac{1,256 \times 1 \times 5.62 \times 0.0165}{6.28 \times 2 \times 56.2}$$

$$\Delta p = 0.165 \text{ psi.}$$

This quantity is much less than can be detected with field instruments. It can be concluded that, although the use of the Theis curve would result in a large percentage error, the absolute magnitude would be small. Continuing this example further, after 1,000 days, $t_0 = 1$ and $\Delta p_0 = 0.53$ or $\Delta p = 5.3$ psi. According to Fig. 4, using the Theis solution would introduce an error of about 2 per cent.

EXAMPLE B

Let us examine another aquifer situation at a smaller radius ratio tc determine if the error that would result from the Their solution would be substantial. We wish to know the pressure drop at a point in an aquifer 10,000 ft from the center of a reservoir with an equivalent radius of 2,500 ft. Assume the following conditions:

$$k = 63.2 \text{ md, or } 0.4 \text{ perms}$$

$$\phi = 0.1 \text{ per cent}$$

$$c = 4 \times 10^{-4} \text{ psi}^{-1}$$

$$\mu = 1 \text{ cp}$$

$$r_{0} = 10,000/2,500 = 4$$

$$t_{0} = \frac{0.4 t}{0.1 \times 1 \times 4 \times 10^{-4} \times 10,000^{2}} = 0.01t.$$

From Fig. 4, at all times greater than t = 490 days, the Theis curve can be used and the error will be 1 per cent or less. However, for times less than t = 120 days, the errors would exceed 5 per cent; and as indicated on Fig. 4 by the location of the 100 per cent error line, these errors would increase rapidly at lower values of time. The absolute magnitude would depend on the other aquifer parameters.

EXAMPLE C

The Theis solution can be used for points in the reservoirs of large radius ratios with little or no error. Let us examine the situation where the distance between wells is 250 ft, and the well radius is 0.5 ft. Assume the following conditions:

k = 158 md, or 1 perm $\phi = 0.2$ per cent

$$c = 8 \times 10^{-4} \text{ psi}^{-1}$$

$$\mu = 0.4 \text{ cp}$$

$$t_{\nu} = \frac{1 t}{0.2 \times 0.4 \times 8 \times 10^{-4} \times 250^{2}} = 25t$$

From Fig. 4, it can be seen that at $r_b = 500$, the Theis solution can be used with an error of 0.1 per cent or less for all values of $t_b > 0.045$. This is equivalent to about 2 minutes. For all practical examples where the radius ratio is large, the Theis solution can be used with confidence.

CONCLUSIONS

1. Solutions for the diffusivity equation for the infinite radial case at constant terminal rate are presented in the form of graphs of dimensionless pressure drop vs dimensionless time for radius ratios from 1 to infinity.

2. For radius ratios of 20 or above, the Theis, or point source, solution can be used with little or no error for most practical situations. A chart is presented where one can determine the order of the errors that will result through use of the Theis solution.

3. In aquifer studies, it might be necessary to use the new solutions of the diffusivity equation presented here for low radius ratios. The absolute magnitude of the pressure effects with low ratios and small times might, however, be insignificant.

4. In well interference tests, the Theis solution can be used for all practical lengths of time, and at all normal well spacings, without introducing errors greater than 0.1 per cent.

NOMENCLATURE

- c = compressibility of fluid, psi⁻¹
- h = reservoir thickness, ft
- k = permeability, md, (1 perm = 158 md)
- p =pressure, psia
- $p_p = \text{dimensionless pressure}$
- $p_* =$ reference pressure, psia
- p_1 = initial pressure at some given point, psia
- p_{z} = pressure at some given point after an elapse of time. psia
- q = constant flow rate at well, B/D
- r = radial distance, ft
- $r_p = \text{dimensionless radius}$
- r_{\bullet} = wellbore radius, ft
- t = time, days
- $t_o =$ dimensionless time
- X = independent variable in Theis solution
- $\mu =$ fluid viscosity, cp
- $\rho =$ fluid density at pressure p, lb/cu ft
- $\rho_n =$ fluid density at pressure p_n , lb/cu ft
- $\phi = \text{porosity}$

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Use of this correlation is illustrated in Example D.17. The result may be of no greater accuracy than simply assuming $c_f = 4 \times 10^{-6}$ psi⁻¹, since only one of the many variables affecting c_f has been taken into account.

Example D.17 – Estimation of Formation Compressibility

Problem. Estimate the formation compressibility c_f for a reservoir with 20% porosity.

Solution. From Fig. D-22, $c_f = 3.6 \times 10^{-6}$ psi⁻¹.

Exercises

Results of pressure transient test analysis sometimes are combined with rock and fluid properties to calculate the folk wing quantities:

Total reservoir flow rate,

 $q_{Rt} = q_o B_o + q_w B_w + (q_g - R_s q_o/1,000) B_g.$ Total mobility: $\lambda_t = k_o / \mu_o + k_w / \mu_w + k_g / \mu_g.$ Total compressibility, $c_t = c_o S_o + c_w S_w + c_g S_g + c_f.$

The following exercises require calculation of q_{Rt} , λ_t , and c_t for two cases.

D.1. Calculate q_{Rt} , λ_t , and c_t for an undersaturated oil reservoir with the following properties.

 $\begin{array}{l} q_o = 100 \, \mathrm{STB/D}, \\ q_w = 20 \, \mathrm{STE/D}, \\ q_g = q_o R_s \mbox{ (reservoir produces dissolved gas only)}, \\ \mbox{Reservoir temperature} = 4,000 \, \mathrm{psia}, \\ \mbox{Reservoir temperature} = 220^\circ \mathrm{F}, \\ R_s = 400 \, \mathrm{scf/STB}, \\ \gamma_g = 0.7, \\ \gamma_o = 0.85, \\ \mbox{Water salinity} = 25,000 \, \mathrm{ppm} \, (2.5\% \, \mathrm{NaCl}), \\ k_o = 20 \, \mathrm{md}, \\ k_w = 0.93 \, \mathrm{md}, \\ k_g = 0 \, (\mathrm{no \ free-gas \ saturation}), \\ \phi = 0.18, \\ S_o = 0.65, \\ S_w = 0.35, \, \mathrm{and} \\ \end{array}$

 $S_g = 0.$

D.2. Calculate q_{Rt} , λ_t , and c_t for a saturated oil reservoir with the following properties:

 $q_0 = 100 \text{ STB/D},$ $q_w = 5 \text{ STB/D},$ $q_g = 250 \text{ Mscf/D},$ Oil gravity = 38°API, Gas gravity = 0.8, Reservoir pressure = 2,000 psia, Reservoir temperature = 200°F, $k_0 = 100 \text{ mJ},$ $k_w = 3.3 \text{ md},$ $k_g = 7.25 \text{ md},$



Fig. D-22 - Formation compressibility.¹⁵

Water salinity = 27,500 ppm, $S_w = 0.25$, $S_g = 0.05$, $S_o = 0.70$, and

$$\phi = 0.18$$
.

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Fig. 6.1 - Pressure response in interference test.



Fig. 6.2 - Region investigated in interference test.



Fig. 6.3 - Exponential integral solution.

and

$$t_D = \frac{0.000264 \, kt}{\phi \mu c_t r_w^2} \, .$$

.

Fig. 6.3 can be used in the following way to analyze interference tests.

1. Plot pressure drawdown in an observation well, $\Delta p = p_i - p_r$, vs. elapsed time t on the same size loglog paper as the full-scale, type-curve version of Fig. 6.3 using an undistorted curve (the reader can prepare such a curve easily).

2. Slide the plotted test data over the type curve until a match is found. (Horizontal and vertical sliding both are required.)

3. Record pressure and time match points, $(p_D)_{MP}, \Delta p_{MP}$ and $[(t_D/r_D^2)_{MP}, t_{MP}]$.

4. Calculate permeability k in the test region from the pressure match point:

$$k = 141.2 \frac{qB\mu}{h} \frac{(p_D)_{\rm MP}}{(\Delta p)_{\rm MP}}$$

5. Calculate ϕc_t from the time match point:

$$\phi c_t = \left(\frac{0.000264 \, k}{\mu r^2}\right) \left[\frac{t_{\rm MP}}{(t_D/r_D^2)_{\rm MP}}\right].$$

Example 6.1 – Interference Test in Water Sand

Problem. An interference test was run in a shallowwater sand. The active well, Well 13, produced 466 STB/D water. Pressure response in shut-in Well 14, which was 99 ft from Well 13, was measured as a function of time elapsed since the drawdown in Well 13 began. Estimated rock and fluid properties include $\mu_w = 1.0 \text{ cp}$, $B_w = 1.0 \text{ RB/STB}$, h = 9 ft, $r_w = 3$ in., and $\phi = 0.3$. Total compressibility is unknown. Pressure readings in Well 14 were as given in Table 6.1. Estimate formation permeability and total compressibility.

Solution. We assume that the aquifer is homogeneous, isotropic, and infinite-acting; we use the *Ei*-function type curves to estimate k and c_1 . Data to be plotted are presented in Table 6.2. The data fit the *Ei*-function type curve well. A pair of match points are ($\Delta t = 128$ minutes, $t_D/r_D^2 = 10$) and ($\Delta p = 5.1$ psi, $p_D = 1.0$). (See Fig. 6.4.) Thus,

$$k = 141.2 \frac{qB\mu}{h} \frac{(p_D)_{\rm MP}}{(\Delta p)_{\rm MP}}$$
$$= \frac{(141.2)(466)(1.0)(1.0)}{(9.0)} \frac{(1.0)}{(5.1)}$$

=1,433 md,

and

$$c_{t} = \frac{0.000264}{\phi r^{2}} \frac{k}{\mu} \frac{(t_{\rm MP}/60)}{(t_{\rm D}/r_{\rm D}^{2})_{\rm MP}}$$

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DETERMINATION OF PORE VOLUME, Ph PRESSURE RESPONDE TO FRAL TREATMENT FROM (BY SUPERPOSITION) BASIC FORMULA: 9= Bbilday $\Delta P = \frac{g \mu B}{14.6 \, \text{Kh}} E \left[\frac{-\hbar^2}{4 \, \text{M} \, \text{K}} \right]$ 4= UIS, 2P B = FVF K = darups h = freit M= 6,328K t = days Q = yorosity, fraction CT= Vor/vor/H n = distance between wells RELOGNIZE TOTAL MOBILITY: Ar = Ko + Ko + Kon (John Lee, ref. 3) Use symbol (KT) FROM CURVE MATCHING OF ET SOLUTION DETERMINE (KE)h and M $\binom{k_{\tau}}{\mu_{\tau}} = \binom{k_{\tau}h}{\mu_{\tau}}$ DIVIDE $\frac{6.328(K)h}{C_T \phi(D_T)} = \mathcal{N}$ (Kr)h x 6.328 FROM NITKH &h= M × Cr


In the frac pulse testing described herein, as well as the other interference tests where a significant amount of free gas is present, the resulting transmissibility determined will be $|K_T| = h$;

and additional information is needed to determine Koh.

It appears that the additional information needed is the producing GOR and PVT properties of Bg, Bo, uo, and ug.

As shown on page 2 following, it appears that the ratio of

(MT) can be determined from only Kg/Ko and the fluid viscos.ties. Since Kg/Ko can be determined from the producing GOR (along with the presumably known quantities, Bg, Bo, uo and ug), then, essent: ally these are the only additional data required for any reservoir. Accordingly Koh can be determined independent of any knowledge of Kg/Ko or Kro relations (John Lee, reference 1).

This unique relation for the approximate PVT properties of West Puerto Chiquito at 1400# reservoir pressure is shown on the graph, page 4, from data calculated on page 3.

DETERMINATION of Kon from/KT/b and Ky/Ko Since, by definition: Kno x K = Ko Then Ky = KyK and Ko Khen Ks = KyK Ko K = Ky and Kg = (Kay)(Ko) = (Kg)Ko Jo that, given Ky/k & Kno, Kng is defined TOTAL MODILITY A = Ke + Kg (John Lee 3) Use symbol KI 50 KT = Ka + Kg = Krok + Krog K HT Ho Hg = Ho + Tg and Kith = (Kn= + Kn=)Kh $Kh = \frac{K_{+}h}{4\pi}$ (Kno + Kny) (Ho + Tra) and rottio Koh Krip = KhxKro= KRO (Kro + Kry) $\left(\frac{1}{4a}+\frac{K_{a}}{K_{a}}\right)$ & finally, ratio = AFP IT - Dage 2

DETERMINATION of how por partie For Reservoir press Koh = darcy feet (K+=) = Ko+Ka $45e_{j10} = .6 \quad B_{b} = 1.28 \quad B_{g} = 5255cf/res bbl$ $k_{s} = 500 cf/bbl \quad M_{g} = .015cp$.015cp .0093 750 .437 .0186 1000 ,344 1500 ,0372 2000,0558 186 2500,0744 1.51 3500 ,1116

(2) $K_{q}/k_{0} = \frac{(R-R_{5})}{B_{0}B_{1}} \times \frac{M_{q}}{M_{0}}$

APP II - Page 3

